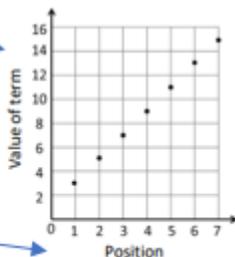


KNOWLEDGE ORGANISER: Year 7 Unit 1 - Sequences

Name	Definition	Example	Non-example
Term	a single number or variable, or numbers and variables multiplied together	5 a 5g d ² c ³ 3a ⁴ -5r	5+12 2a+3 6-4x ² 17-2r
Pattern	A series of terms, objects or colours that repeat themselves	a, b, c, a, b, c, a, b, c... 1, 2, 1, 2, 1, 2, 1, 2... m, t, w, t, f, s, s, m, t, w, t, f, s, s...	1, 2, 3, 4, 5... (π) 3.141519... $\sqrt{2} = 1.41421...$
Sequence	A succession of terms generated by following a rule	1, 3, 5, 7, 9... 2, 4, 6, 8, 10... 1, 4, 9, 16, 25, 36...	1, 2, 3, 1, 2, 3, 1, 2, 3... Red, blue, red, blue...
Position	Where a number is in the sequence	In the sequence 5, 10, 15, 20, 25... The first (1 st) number/position is 5 The fourth (4 th) number/position is 20	
Common Difference Or Term-to-term rule	The difference between any two consecutive terms in a sequence	The common difference of 1, 4, 7, 10 is 3	1, 4, 5, 8, 9, 12, 13... has no common difference
General Rule Or n th term	An algebraic expression giving the rule to find any number in the sequence	The n th term of 3, 7, 11, 15 is 4n-1	1, 4, 5, 8, 9, 12, 13... add three then add 1 is not a general rule
Linear Or Arithmetic	A sequence that has a constant common difference	3, 6, 9, 12, 15 is an arithmetic/linear sequence as it goes up by 3 every time 100, 95, 90, 85 is an arithmetic/linear sequence as it decreases by 5 every time	
Non-linear	A sequence that does not have a constant term-to-term rule, including quadratic, Fibonacci and geometric sequences	2, 8, 18, 32, 50... 2, 5, 7, 12, 19, 31... 3, 12, 48, 192...	See linear examples
Ascending	A set of numbers that increase in size	1, 2, 3, 4, 5...	-1, 0, 1, 0, -1, 0, 1...
Descending	A set of numbers that decrease in size	5, 1, -3, -7...	10, 9, 8, 7, 8, 9
Fibonacci	A sequence where the next term is generated by adding the previous two terms together	1, 1, 2, 3, 5, 8, 13 The next term will be 21, because 8+13=21	1, 2, 2, 4, 8, 32
Geometric	A sequence where the term-to-term rule involves multiplying or dividing by the same number each time	1, 3, 9, 27, 81... each term is multiplied by 3 to get the next term 100, 50, 25, 12.5... each term is divided by 2 to get the next term	
Quadratic	A sequence where the second common difference is always the same	1, 4, 9, 16, 25... +3 +5 +7 +9 +2 +2 +2	the sequence first differences second differences

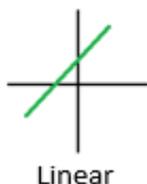
Vertical axis is called the y-axis

Horizontal axis is called the x-axis



“Ascending” means to go up
“Descending” means to go down

Linear functions result in a straight line graph



Linear

Substitution:

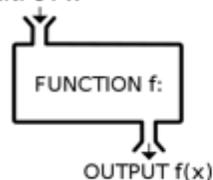
- Replace letters with values
- Always apply BIDMAS
- Use brackets for powers
- Fractions? Work out the top and bottom separately.

If $p = 5$,
What is the value of
 $2p + 9$?

ANSWER-
 $2 \times 5 + 9 = 19$

Algebraic Notation 1

INPUT x



A “Function” machine takes an **input**, applies a **rule** (operation) then delivers an answer, **output**.

The four basic **operations** are $+ - \times \div$

Two step function machine has two operations



Find the output in each of these function machines when the input is 15

$$15 \longrightarrow \boxed{+1000} \longrightarrow \underline{\underline{1015}}$$

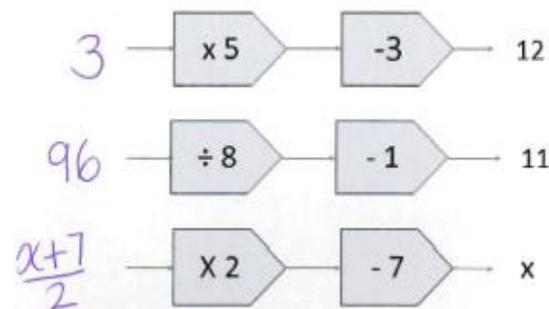
$$15 \longrightarrow \boxed{-9.2} \longrightarrow \underline{\underline{5.8}}$$

Algebra and function machines

$$\begin{array}{l} x \longrightarrow \boxed{+2} \longrightarrow \underline{\underline{x + 2}} \\ x + 3 \longrightarrow \boxed{+2} \longrightarrow \underline{\underline{x + 5}} \end{array}$$

Finding the INPUT

2. Find the missing inputs for these function machines



Sequences

Sequence:



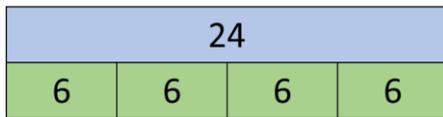
A “Sequence” is a succession of terms formed according to a rule
“Terms” are the numbers in a sequence

Find the n^{th} term of the linear sequence: 8, 11, 14, 17, ...



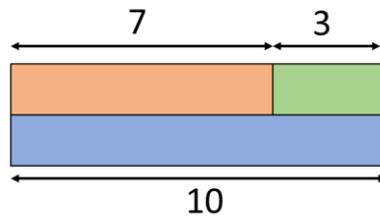
KNOWLEDGE ORGANISER: Year 7 Unit 3 – Equality & Equivalence

Bar Models and Fact Families



Fact family for this bar model:

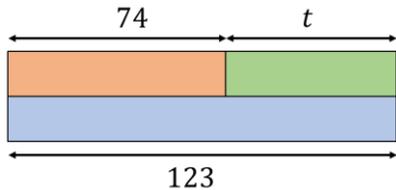
$$\begin{aligned} 6 \times 4 &= 24 & 24 &= 6 \times 4 \\ 4 \times 6 &= 24 & 24 &= 4 \times 6 \\ 24 \div 4 &= 6 & 6 &= 24 \div 4 \end{aligned}$$



Fact family for this bar model:

$$\begin{aligned} 7 + 3 &= 10 & 10 &= 7 + 3 \\ 3 + 7 &= 10 & 10 &= 3 + 7 \\ 10 - 7 &= 3 & 3 &= 10 - 7 \\ 10 - 3 &= 7 & 7 &= 10 - 3 \end{aligned}$$

Equations



The bar model shows this equation:

$$74 + t = 123$$

The solution is:

*Ellie thinks of a number.
She adds 15.
The answer is 87.*

This can be written as an equation:

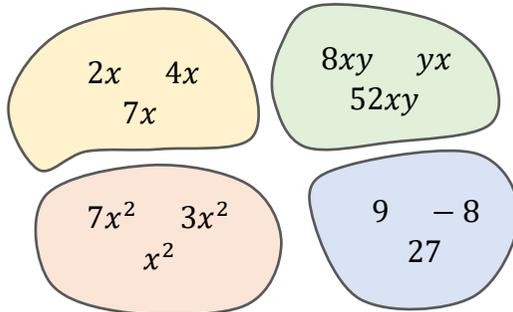
$$n + 15 = 87$$

Like terms

Each group contains related terms – **like terms**.

Can you see which group each of these terms would go in:

$$5x \quad 3xy \quad x$$



KEY WORDS & DEFINITIONS

equality, equals, equal to	The same. eg. $16 - 3 = 13$, $5 + 6 = 8 + 3$
equation	A fact which can be solved to find a mystery number e.g. $x + 5 = 9$ has solution $x = 4$
fact family	A group of connected number facts e.g. $5 + 3 = 8$ and $8 - 3 = 5$ are connected.
like terms	Terms that are the same type. e.g. $5a$ and $3a$, 9 and 7 , $3x^2$ and $4x^2$
substitute	replace the letter with a number e.g. if $g = 5$ then $2g = 2 \times 5 = 10$
identity	A mathematical statement that is <i>always</i> true. e.g. $5x + 2x = 7x$ is true whatever value x has. We often use this special symbol for an identity: \equiv
simplify	Write in the simplest possible way e.g. $h + h + h$ can be simplified to $3h$

Collecting like terms

Expressions can be simplified by collecting like terms together.
Here are some examples:

$$a + a + a + a = 4a$$

$$2a + a + 3b + b = 3a + 4b$$

$$5x + 7x - 2x = 10x$$

$$2h + 5 + h + 6 = 3h + 11$$

$$3p^2 + 4p - p^2 = 2p^2 + 4p$$

Substitution

The letter (unknown) is replaced with a value.

e.g. if $k = 3$ then:

$$k + 5 = 3 + 5 = 8$$

$$2k = 2 \times 3 = 6$$

$$10 - k = 10 - 3 = 7$$

$$k^2 = 3^2 = 3 \times 3 = 9$$

YEAR 7 POWER PACK 1

KNOWLEDGE IS POWER!

Seven times tables

$$1 \times 7 = 7$$

$$2 \times 7 = 14$$

$$3 \times 7 = 21$$

$$4 \times 7 = 28$$

$$5 \times 7 = 35$$

$$6 \times 7 = 42$$

$$7 \times 7 = 49$$

$$8 \times 7 = 56$$

$$9 \times 7 = 63$$

$$10 \times 7 = 70$$

$$11 \times 7 = 77$$

$$12 \times 7 = 84$$

Sequences

A “**Sequence**” is a succession of terms formed according to a rule

“**Terms**” are the numbers in a sequence

“**Term to term rule**” lets you find the next term in a sequence if you know the previous term

“**Difference**” is the numerical difference between two numbers

e.g. difference in between 8 and 5 is $8 - 5 = 3$

A **linear sequence (arithmetic sequence)** is a number pattern which increases (or decreases) by the same amount each time. The amount it increases or decreases by is known as the **common difference**.

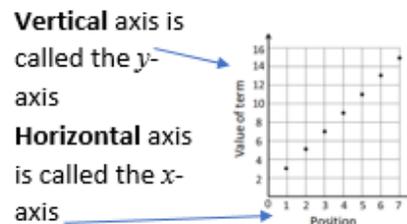
A **non-linear sequence** is a number pattern which does not increase (or decrease) by the same amount.

Geometric sequences multiply (or divide) by the same value each time.

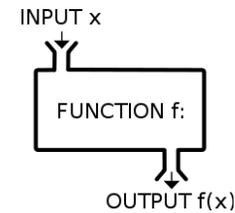
Fibonacci sequences are formed by adding the previous two terms.

“**Ascending**” means to go up

“**Descending**” means to go down



Algebraic Notation 1



A “**Function**” machine takes an **input**, applies a rule (operation) then delivers an answer, **output**.

The four basic **operations** are $+ - \times \div$

To **square** a number is to multiply a number by itself e.g. The square of 5 is $5 \times 5 = 5^2 = 25$

Inverse operations are the opposite operations e.g. the inverse of multiplication is division

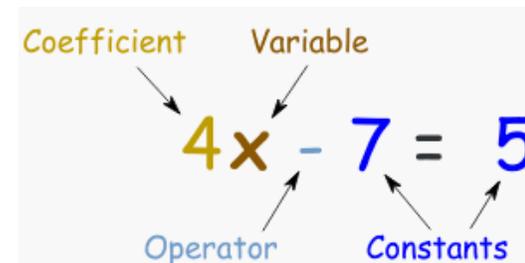
“**Expressions**” are made up of terms which may include letters, number and operators

e.g. ab^2 , $ab + 5$ and $4d - 5$

Variable is a quantity that can take on a range of values, often denoted by a letter, x , y etc.

Coefficient is the number in front of a variable

Constant is a number or quantity that does not vary



Algebraic Notation 2

Commutative is where a calculation can be done in any order to give the same result
e.g. $5 \times 4 = 4 \times 5$ $6 + 3 = 3 + 6$

Substitute is where we replace a letter with a number.

Evaluate means to calculate the value of.
e.g. if $y = 7$ evaluate $5y$. Answer $5 \times 7 = 35$

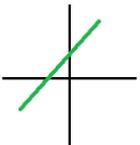
Brackets are used in pairs to group things together e.g. $2(x + 1)$ is two lots of $x + 1$

Equation is a statement that two things are equal, it contains expressions on both sides of the equal sign. e.g. $5 = 2x + 1$

Two step function machine has two operations

Consecutive numbers are numbers which follow in order without gaps. e.g. 12, 13, 14...

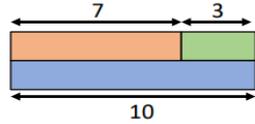
Linear functions result in a straight line graph



Equality and Equivalence

Equality means having the same value
e.g. 1minute = 60 seconds

Fact families are a group of maths facts using the same numbers



$$\begin{aligned}7 + 3 &= 10 \\7 &= 10 - 3 \\10 - 7 &= 3\end{aligned}$$

Unknown is another word for a variable, a value we don't know yet. The Unknown has one distinct value

When we **solve** an equation we find the value of the unknown

e.g. solve $x + 5 = 8$ answer $x = 3$

In the above example $x = 3$ is the **solution** (answer)

We solve equations by doing the **inverse** operation

Terms in algebra are single numbers, variables or product of several numbers and variables

Product is the result when you multiply one number by another. Product of 4 and x is $4x$.

Equality and Equivalence 2

Like terms contain the same variable
e.g. $4a$ and $-2a$ or 8 and 13 or $9m^2$ and $3m^2$

Unlike terms do not contain the same variable e.g. $4y$ and $3x$ are unlike terms

Equivalent \equiv means of equal value
e.g. $2x + 3x \equiv 5x$ is true for all values of x

We can **simplify** an expression by **collecting** like terms. e.g. $7a + 5b - 2a + b \equiv 5a + 6b$

A mathematical **convention** is an agreed way of doing something in maths e.g. we write $3 \times y$ as $3y$ not $y3$

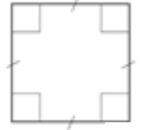
The **Index** of a number tells you how many times to multiply the number by itself

e.g. y^3 means $y \times y \times y$.

We say y^3 as "y to the power of 3" or y cubed

m^2 ^{Index}

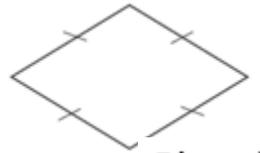
Indices is the plural of index



Square



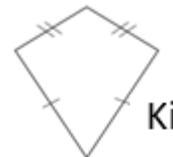
Rectangle



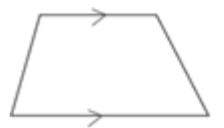
Rhombus



Parallelogram



Kite



Trapezium

YEAR 7 — PLACE VALUE AND PROPORTION... FDP equivalence

What do I need to be able to do?

By the end of this unit you should be able to:

- Convert fluently between fractions, decimals & percentages

Keywords

Fraction: how many parts of a whole we have

Decimal: a number with a decimal point used to separate ones, tenths, hundredths etc.

Percentage: a proportion of a whole represented as a number between 0 and 100

Place value: the numerical value that a digit has decided by its position in the number

Placeholder: a number that occupies a position to give value

Interval: a range between two numbers

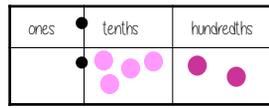
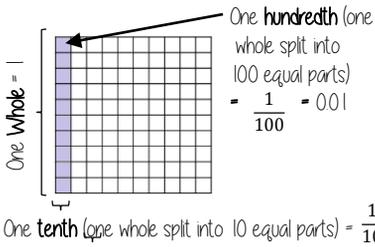
Tenth: one whole split into 10 equal parts

Hundredth: one whole split into 100 equal parts

Sector: a part of a circle between two radius (often referred to as looking like a piece of pie)

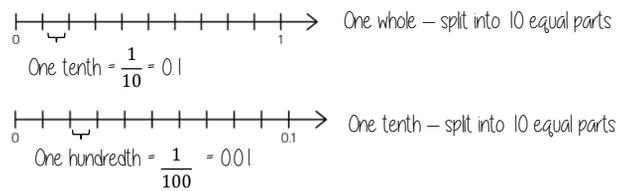
Recurring: a decimal that repeats in a given pattern

Tenths and hundredths

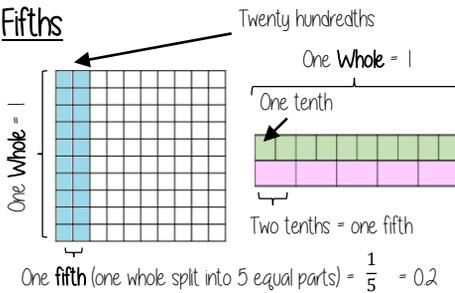


0 ones, 5 tenths and 2 hundredths
 $0 + 0.1 + 0.1 + 0.1 + 0.1 + 0.01 + 0.01$
 $= 0 + 0.5 + 0.02$
 $= 0.52$

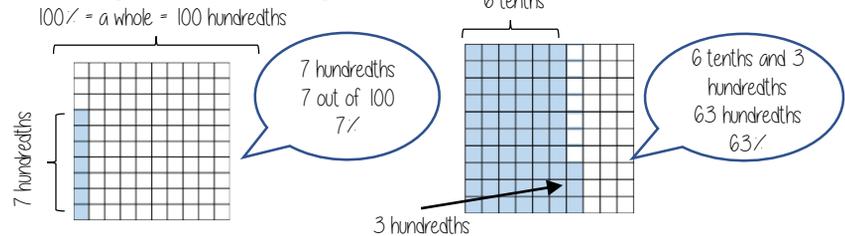
On a number line



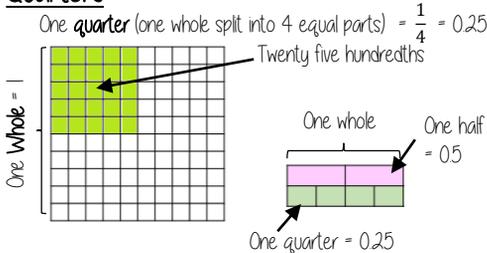
Fifths



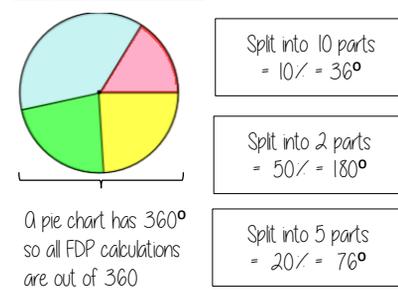
Percentages on a hundred grid



Quarters

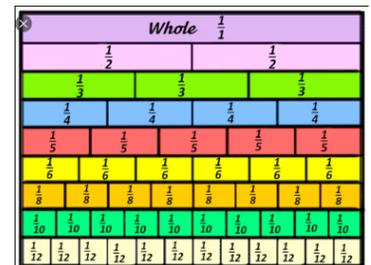


Simple pie charts

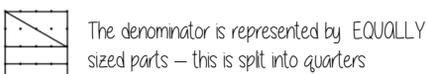


Equivalent fractions

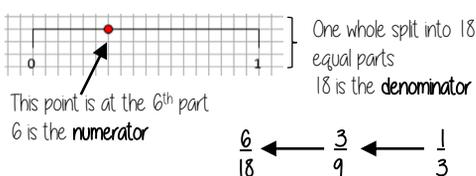
Represent equivalence with fraction walls



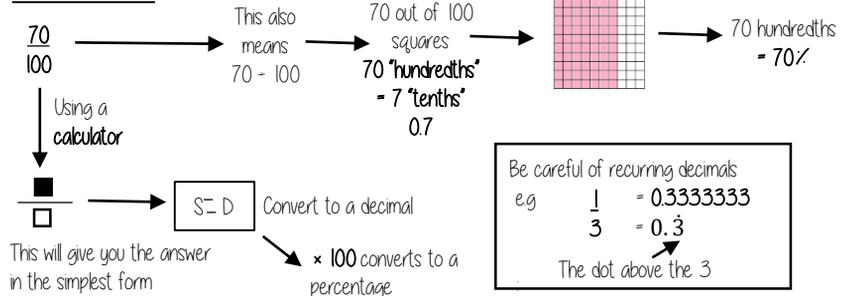
Fractions — on a diagram



Fractions — on a number line



Convert FDP



Be careful of recurring decimals
 e.g. $\frac{1}{3} = 0.3333333$
 $\frac{1}{3} = 0.\dot{3}$
 The dot above the 3

Six times tables

$$1 \times 6 = 6$$

$$2 \times 6 = 12$$

$$3 \times 6 = 18$$

$$4 \times 6 = 24$$

$$5 \times 6 = 30$$

$$6 \times 6 = 36$$

$$7 \times 6 = 42$$

$$8 \times 6 = 48$$

$$9 \times 6 = 54$$

$$10 \times 6 = 60$$

$$11 \times 6 = 66$$

$$12 \times 6 = 72$$

Digit is one of the symbols from 0,1,2,3,4,5,6,7,8,9.

Integers are whole numbers, e.g. 4, 270, -6. They are not decimals or fractions.

Place Value is the value of the digit that is related to it's position on a number line.

Place Holder The zero number is used as a place holder to show that a place value is zero. E.g. 502 without a place holder to show there are no tens would be mistaken for 52.

Billion = 1 000 000 000

Intervals are **spaces** on a number line which are split through **equal division**.

Round is when we write a number to a required degree of accuracy e.g. 543 rounded to the nearest 10 is 540. The **convention** in Maths is to round up if we are **halfway** e.g. 25 to the nearest 10 is 30 because 25 is halfway between 20 and 30.

Convention means a way in which something is usually done.

Approximate is a number that is not exact but close to the actual number for it to be useful.

= Equal

≠ Not equal

> Greater than

≥ Greater than or equal to

< Less than

≤ Less than or equal to

≡ Identical to

Leading digit is the first digit in a number e.g. the number 3042 has the leading digit of 3.

One significant figure means have just one leading digit for a number. Leading zero's are not significant.

Difference is the result of subtracting one number from another e.g. the difference between 8 and 17 is 9 (17-8=9).

Greatest number is the largest number.

Least number is smallest number.

Range is difference between the largest and smallest values.

Median is the middle number when all the numbers are arranged in ascending order. Median is an example of an **average**.

10^5 means 10 to the power 5 which is $10 \times 10 \times 10 \times 10 \times 10$. The 5 is called the **index**.

*H***Standard form** is a way of writing numbers so that they are between 1 and 10 and multiplied by a **power** of 10 e.g. 8000 is 8×10^3

*H***Scientific Notation** is another word for Standard form. Standard form is used in science to express very large or very small numbers.

Percent is a fraction out of a hundred
e.g. 15% is $\frac{15}{100}$

Equivalent means the same value
e.g. $\frac{1}{4} = \frac{2}{8}$

Convert means to change from one quantity to another, e.g. convert fractions to percentages.

Recurring: a decimal that repeats in a given pattern

$$\text{Tenth} = \frac{1}{10} = 0.1 = 10\%$$
$$\text{Hundredth} = \frac{1}{100} = 0.01 = 1\%$$

$$\text{Fifth} = \frac{1}{5} = 0.2 = 20\%$$
$$\text{Quarter} = \frac{1}{4} = 0.25 = 25\%$$
$$\text{*H*Eighth} = \frac{1}{8} = 0.125 = 12.5\%$$

The **numerator** is the top number in a fraction. It tells us how many parts we have.

The **denominator** is the bottom number in a fraction. It shows how many parts the item has been split into.

$$\frac{3}{5}$$

← numerator
← denominator

Dividend is the number that is being divided.

Divisor is the number that you are dividing by.

Quotient is the result of a division.

$$\begin{array}{r} 6 \leftarrow \text{quotient} \\ 4 \overline{) 24} \leftarrow \text{dividend} \\ \underline{4} \\ 0 \end{array}$$

↑
divisor

Interval: a range between two numbers.

Improper fractions have a numerator greater than the denominator.

Mixed fractions contain a whole number and a fraction.

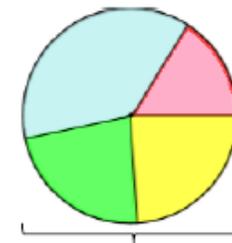
$$2\frac{1}{2} \rightarrow \frac{5}{2}$$

Mixed fraction Improper fraction

A **Pie Chart** is a type of graph in which a circle is divided into sectors that each represent a proportion of the whole.

Sector is a part of a circle between two radius (often referred to as looking like a piece of pie)

Simple pie charts

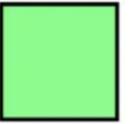


Split into 10 parts
= 10% = 36°

Split into 2 parts
= 50% = 180°

Split into 5 parts
= 20% = 76°

A pie chart has 360°
so all FDP calculations
are out of 360



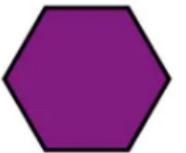
quadrilateral

4 Sides



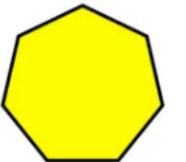
pentagon

5 Sides



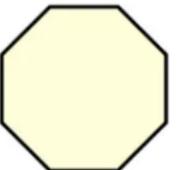
hexagon

6 Sides



heptagon

7 Sides



octagon

8 Sides

YEAR 7 — APPLICATION OF NUMBER

Solving problems with addition and subtraction

@whisto_maths

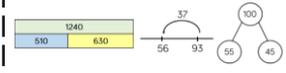
What do I need to be able to do?

- By the end of this unit you should be able to:
- Understand properties of addition/ subtraction
 - Use mental strategies for addition/subtraction
 - Use formal methods of addition/subtraction for integers
 - Use formal methods of addition/subtraction for decimals
 - Solve problems in context of perimeter
 - Solve problems with finance, tables and timetables
 - Solve problems with frequency trees
 - Solve problems with bar charts and line charts

Keywords

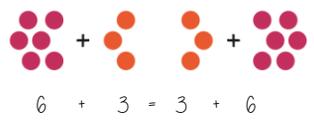
- Commutative:** changing the order of the operations does not change the result
- Associative:** when you add or multiply you can do so regardless of how the numbers are grouped
- Inverse:** the operation that undoes what was done by the previous operation (The opposite operation)
- Placeholder:** a number that occupies a position to give value
- Perimeter:** the distance/ length around a 2D object
- Polygon:** a 2D shape made with straight lines
- Balance:** in financial questions — the amount of money in a bank account
- Credit:** money that goes into a bank account
- Debit:** money that leaves a bank account

Addition/ Subtraction with integers



- Modelling methods for addition/ subtraction
- Bar models
 - Number lines
 - Part/ Whole diagrams

Addition is commutative



The order of addition does not change the result

Subtraction the order has to stay the same

$$360 - 147 = 360 - 100 - 40 - 7$$

- Number lines help for addition and subtraction
- Working in 10's first aids mental addition/ subtraction
- Show your relationships by writing fact families

Formal written methods

	H	T	O
	1	8	7
+	5	4	2

	H	T	O	
		4	2	7
-		2	4	9

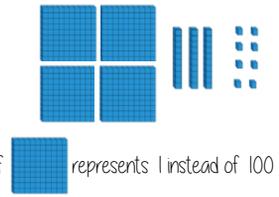
Remember the place value of each column. You may need to move 10 ones to the ones column to be able to subtract.

Addition/ Subtraction with decimals

0 can be used to fill empty places with value

4	.	3	8
7	.	9	0
			+

The decimal place acts as the placeholder and aligns the other values

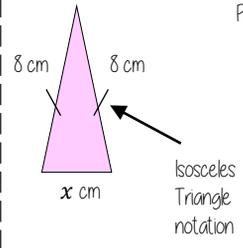


$$5.43 + \frac{8}{10}$$

Revisit Fraction — Decimal equivalence
 $5.43 + 0.8$

Solve problems with perimeter

Perimeter is the length around the outside of a polygon



The triangle has a perimeter of 25cm. Find the length of x .

$$8\text{cm} + 8\text{cm} + x\text{cm} = 25\text{cm}$$

$$16\text{cm} + x\text{cm} = 25\text{cm}$$

$$x\text{cm} = 9\text{cm}$$

Solve problems with finance

- Profit = Income - Costs
- Credit — Money coming into an account
- Debit — Money leaving an account

Money uses a two decimal place system
14.2 on a calculator represents £14.20

Check the units of currency — work in the same unit

Tables and timetables

Distance tables

London		Cardiff	Glasgow	Belfast
211	556	493	518	177
392				

This shows the distance between Glasgow and London. It is where their row and column intersects

Bus/ Train timetables

Harton	1005	1045	1130
Bridge	1024	1106	1147
Aville	1051	1133	1205
Ware	1117	1202	1233

Each column represents a journey, each row represents the time the 'bus' arrives at that location

TIME CALCULATIONS — use a number line

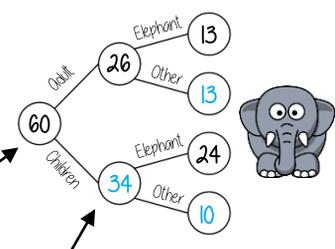
Two-way tables

	H	T
H	HH	HT
T	TH	TT

Where rows and columns intersect is the outcome of that action

Frequency trees

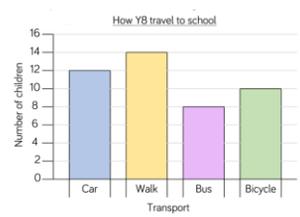
60 people visited the zoo one Saturday morning
26 of them were adults. 13 of the adult's favourite animal was an elephant. 24 of the children's favourite animal was an elephant



The overall total "60 people"

Probabilities or statements can be taken from the completed trees
e.g. 34 children visited the zoo

Bar and line charts

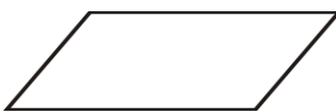
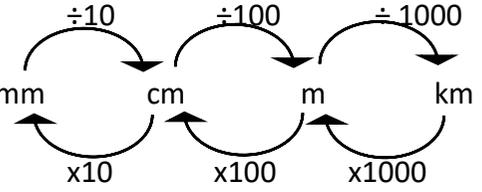
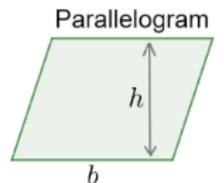
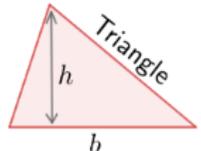
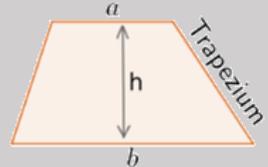


Use addition/ subtraction methods to extract information from bar charts

e.g. Difference between the number of students who walked and took the bus
Walk frequency — bus frequency

- When describing changes or making predictions:
- Extract information from your data source
 - Make comparisons of difference or sum of values
 - Put into the context of the scenario

KNOWLEDGE ORGANISER: Year 7 Unit 7 – Solving problems with multiplication and division

<p>KEYWORDS</p> <p>Product: To multiply Quotient: The answer to a division Divisor: The value you are dividing by Dividend: The value being divided Inverse: To opposite operation e.g. multiply is the inverse of divide Factor: An integer that can be divided into a value Multiple: An integer that is in a values times table Integer: A whole number Perpendicular: 2 straight lines that meet at 90° {at right angles} Parallel: 2 straight lines that never meet Parallelogram:</p>  <p>Trapezium:</p>  <p>Mean: Add all the data and divide by the amount of pieces of data Mode: The most common piece of data Fraction: Part of a whole number Numerator: The number on the top of a fraction Denominator: The number on the bottom of the fraction Percentage: out of 100 Coefficient: The number multiplying a letter e.g. $3x - 3$ is the coefficient</p>	<p>FRACTION OF AMOUNT</p> <p>$\left\{ \begin{array}{l} \div \text{ by the bottom} \\ \times \text{ by the top} \end{array} \right\}$</p> <p>e.g. $\frac{5}{7}$ of 42 $42 \div 7 = 6$ $6 \times 5 = 30$</p>	<p>LCM</p> <p>Lowest Common Multiple</p> <p>List the multiples, e.g. 3: 3 6 9 12 15 4: 4 8 12</p>	<p>MEAN</p> <p>Add and divide</p> <p>e.g. 3 5 6 6 7 8 $3 + 5 + 6 + 6 + 7 + 8 = 36$ $36 \div 6 = 6$</p>
	<p>PERCENTAGE OF AMOUNT</p> <p>10% : $\div 10$ 5%: half 10% 20%: double 10% 50%: $\div 2$ 25%: $\div 4$ 75%: 50% + 25%</p> <p>e.g. 16% of 300 = 48 $10\% = 300 \div 10 = 30$ $5\% = 30 \div 2 = 15$ $1\% = 300 \div 100 = 3$</p>	<p>HCF</p> <p>Highest Common Factor</p> <p>List all the factors, following a logical pattern e.g. 12: 1 2 3 4 6 12 32: 1 2 4 8 16 32</p>	<p>UNITS</p> <p>1cm = 10mm 1kg = 1000g 1m = 100cm 1km = 1000m</p> 
	<p>Area Formulae</p> <p>Rectangle</p>  <p>Area = base x perpendicular height $= b \times h$ $= bh$</p> <p>Parallelogram</p>  <p>Area = base x perpendicular height $= b \times h$</p>	<p>Area Formulae</p> <p>Triangle</p>  <p>Area = base x perpendicular height $= \frac{b \times h}{2}$</p> <p>Trapezium</p>  <p>Area = $\frac{(a + b)h}{2}$</p> <p>$\left\{ \begin{array}{l} 1\} \text{ Add the parallels} \\ 2\} \text{ Multiply by the difference between} \\ 3\} \div 2 \end{array} \right\}$</p>	<p>DECIMALS</p> <p>MULTIPLYING</p> <p>Don't put decimals in column multiplication, x10, x100, x1000 etc. first, then at the end divide.</p> <p>e.g. 0.32×0.4 $\times 100 \quad \times 10 = \times 1000$ CAN BE MULTIPLE VALUES $32 \times 4 = 128$ $128 \div 1000 = 0.128$</p> <p>DIVIDING</p> <p>Don't put decimals outside the bus-stop</p> <p>e.g. 0.32×0.8 $\times 100 \quad \times 100$ MUST BE SAME VALUES $32 \div 80 = 0.4$</p>

Eight times tables

- $1 \times 8 = 8$
- $2 \times 8 = 16$
- $3 \times 8 = 24$
- $4 \times 8 = 32$
- $5 \times 8 = 40$
- $6 \times 8 = 48$
- $7 \times 8 = 56$
- $8 \times 8 = 64$
- $9 \times 8 = 72$
- $10 \times 8 = 80$
- $11 \times 8 = 88$
- $12 \times 8 = 96$

Sum is the total of **adding** two or more numbers e.g
The sum of 8 and 3 is 11 ($8+3=11$)

Difference is the result of **subtracting** one number from another e.g. the difference between 8 and 17 is 9. ($17-8=9$)

Commutative:

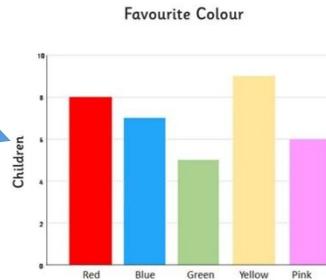
Adding is commutative because $2 + 7 = 9$ and $7 + 2 = 9$
It doesn't matter which way round you add
Subtracting is not commutative because $5 - 2 = 3$
but $2 - 5 = -3$

Associative means we can complete the calculation in any order
 $(4 + 7) + 1 = 4 + (7 + 1)$
 $11 + 1 = 4 + 8$

Bar charts

The height of the bar chart tells you the frequency. Bars must be of equal widths and have equal gaps between them

Frequency on the vertical axis



Data categories on the horizontal axis

Credit is money going into a bank account.

Debit is money going out of a bank account

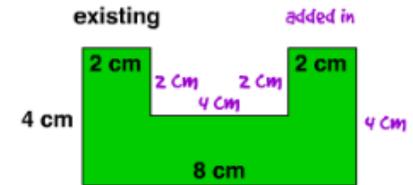
Balance is how much money is in an account

Profit: Sam bought a car for £3000 and sold it for £4000. He made a £1000 profit ($4000 - 3000 = 1000$)

Loss: Sam bought a car for £3000 and sold it for £2000. He made a £1000 loss ($2000 - 3000 = -1000$)

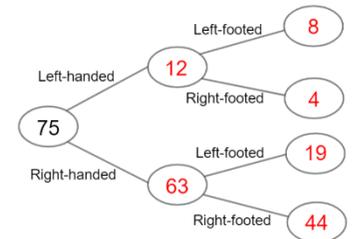
Perimeter is the distance around the outside of a shape.

Some lengths may not be shown on examples.
Don't forget to add them in when calculating perimeter.



$$P = 4 + 2 + 2 + 4 + 2 + 2 + 4 + 8 = 28 \text{ cm}$$

A **frequency tree** is a part whole model.
One piece of information leads to another.



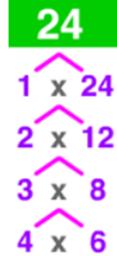
Product: When you multiply two or more numbers the answer is the product.

Multiplication is **commutative** and **associative**.

$6 \times 4 = 24$ $4 \times 6 = 24$, $(7 \times 2) \times 3 = 7 \times (2 \times 3)$

When a number can be written as a product of two numbers, these are **factors**.

Eg factors of 24



Highest common factor (HCF) is the common factor of two or more numbers which has the highest value

Multiples of a number are found by multiplying that number by an integer.

Lowest common multiple (LCM) is the common multiple of two or more numbers which has the least value.

The **mean** is an average.

The mean is the total of all the scores or amounts, divided by, how many scores or amounts there were.

Metric units are units that use powers of ten.

Prefix is a word at the front of another word that changes its meaning.

Units of **Length**

Millimetre (mm)-thickness of a credit card

Centimetre (cm)-width of a paper clip

Metre (m) - width of a school desk

Kilometre (km) -around the length of ten football pitches.

Units of **weight**

Gram (g) - about the weight of one paper clip

Kilogram (kg) - weight of a bag of sugar.

Units of **capacity**

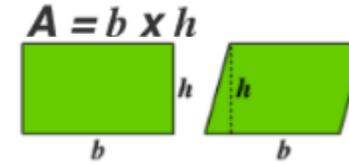
Millilitre (ml) -tip of a teaspoon

Litre (L) - approximately two pints of milk

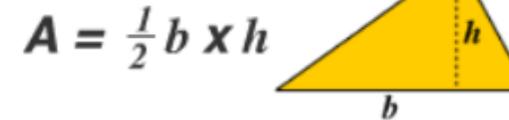
Prefix	Meaning
Milli	$\frac{1}{1000}$
Centi	$\frac{1}{100}$
Deci	$\frac{1}{10}$
Deca	10
Hecto	100
Kilo	1000

The **area** of a shape is the space inside it. It is measured in square units. (mm^2 , cm^2 , m^2 , km^2)

Rectangle and Parallelogram

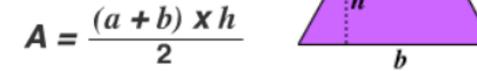


Triangle

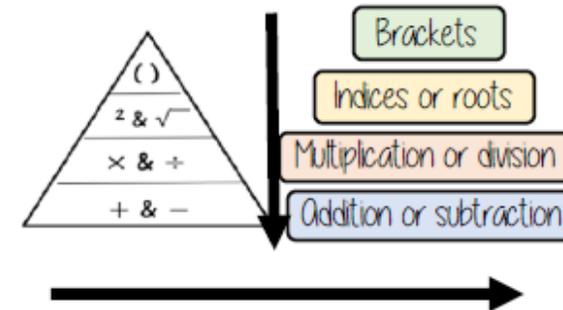


H

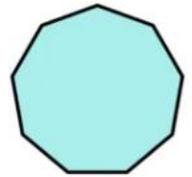
Trapezium



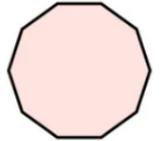
The **order of operations** is the convention for which part of calculations we complete first.



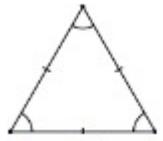
If there are multiple operations from the same tier, work left to right.



nonagon
9 Sides



decagon
10 Sides



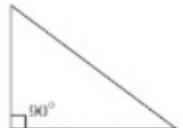
Equilateral Triangle



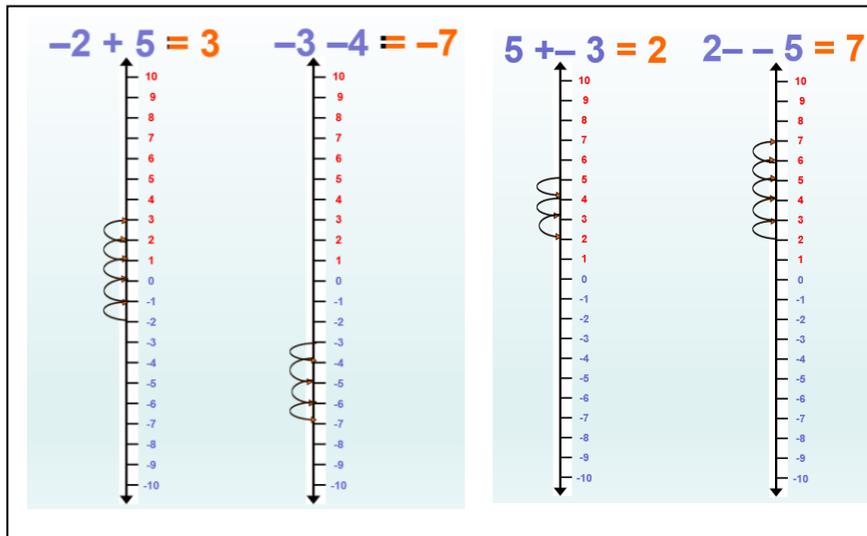
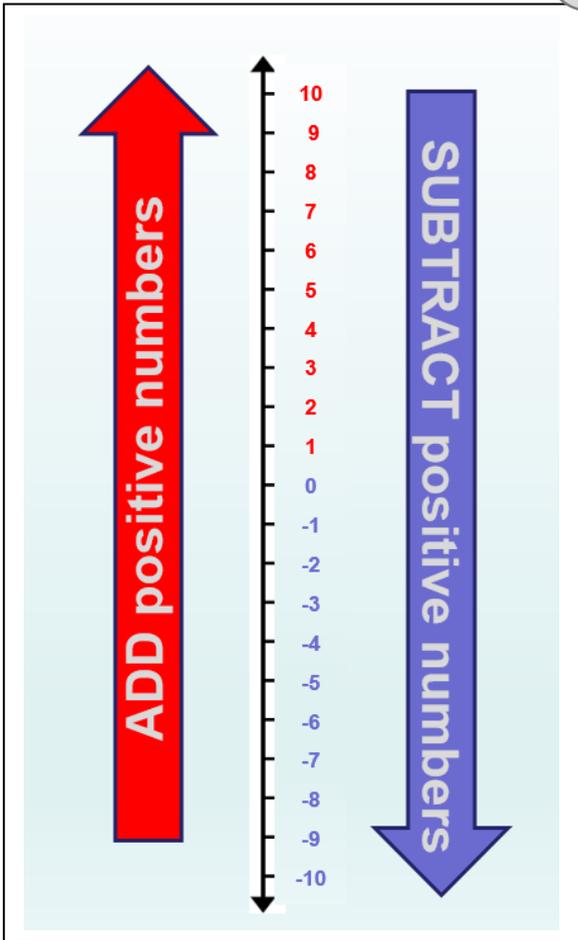
Isosceles Triangle



Scalene Triangle



Right Triangle



Substitution:

- Replace letters with values
- Always apply BIDMAS
- Use brackets for powers
- Fractions? Work out the top and bottom separately.

Key Words:

Positive – numbers greater than zero
 Negative – numbers less than zero
 Increase – gets bigger
 Decrease – gets smaller
 Sum – add the numbers together
 Difference – subtract the smallest from the biggest
 Product – multiply the numbers together

e.g **Evaluate** (find the **value** of) the expressions, given that:
 $a = 2$, $b = 3$, $c = -5$

- $4b = 4 \times 2 = 8$
- $7b - 3c = (7 \times 3) - (3 \times -5) = 21 - 15 = 21 + 15 = 36$
- $5b^2 + 1 = 5 \times (3)^2 + 1 = 5 \times 9 + 1 = 45 + 1 = 46$
- $2c^3 = 2 \times (-5)^3 = 2 \times -125 = -250$
- $\frac{3ac}{2b} = \frac{3 \times 2 \times -5}{2 \times 3} = \frac{-30}{6} = -5$

Multiplying and Dividing Directed Numbers

×	-2	-1	0	1	2
-2	4	1	0	-1	-4
-1	2	1	0	-1	-2
0	0	0	0	0	0
1	-2	-1	0	1	2
2	-4	-2	0	2	4

Negative x Negative = Positive
 Positive ÷ Negative = Negative

Negative x Positive = Negative
 Negative ÷ Positive = Negative

Positive x Negative = Negative
 Negative ÷ Negative = Positive

Positive x Positive = Positive
 Positive ÷ Positive = Positive

Simplifying expressions (adding/subtracting)

- Can only simplify like terms.
- Be sure to include the sign before the term

e.g. $2a + 3b - a + 4b = a + 7b$

$2a - a = a$ $+3b + 4b = +7b$

$$\frac{3}{5}$$

← numerator

← denominator

Linked Prior Topics
 Equivalent fractions, Improper fractions,
 Times table facts, Mixed numbers,
 Lowest common multiples.

Adding and Subtracting

- The denominators must be the same.
- In order to do this find the lowest common multiple for each denominator.
- Remember to multiply the numerator and denominator by the same number.
- Then add the fractions together.

Remember to simplify your answers

When calculating with mixed numbers, you must convert them to improper fractions first.

Mixed numbers to improper fractions

- Multiply the number by the denominator
- Add this to the numerator

Then add.

$$4\frac{1}{3} = \frac{13}{3}$$

Multiply.

Improper fractions to mixed numbers

- Divide the numerator by the denominator
- The remainder is now the numerator

$$\frac{15}{7} \rightarrow 7 \overline{)15}$$

$$7 \overline{)15} \rightarrow 7 \overline{)15} \begin{array}{r} 2 \\ -14 \\ \hline 1 \end{array}$$

Answer = $2\frac{1}{7}$

$$\frac{1}{7} + \frac{4}{7} = \frac{5}{7}$$

$$\frac{4}{5} - \frac{1}{5} = \frac{3}{5}$$

$$\frac{13 \times 2}{12 \times 2} + \frac{17 \times 3}{8 \times 3} = \frac{26}{24} + \frac{51}{24}$$

$$\frac{2}{3} - \frac{2}{11}$$

The LCM of 3 and 11 is 33

$$\frac{2}{3} = \frac{?}{33} \quad \leftarrow 2 \times 11 = 22$$

$$\frac{2}{11} = \frac{?}{33} \quad \leftarrow 2 \times 3 = 6$$

$$\frac{22}{33} - \frac{6}{33} = \frac{16}{33}$$

$$3\frac{2}{5} + 1\frac{4}{7} = \frac{17}{5} + \frac{11}{7}$$

change to improper fractions

$$= \frac{17 \times 7}{5 \times 7} + \frac{11 \times 5}{7 \times 5} = \frac{119}{35} + \frac{55}{35}$$

change to the LCD of 35

$$= \frac{119 + 55}{35} = \frac{174}{35}$$

9 times tables

$$1 \times 9 = 9$$

$$2 \times 9 = 18$$

$$3 \times 9 = 27$$

$$4 \times 9 = 36$$

$$5 \times 9 = 45$$

$$6 \times 9 = 54$$

$$7 \times 9 = 63$$

$$8 \times 9 = 72$$

$$9 \times 9 = 81$$

$$10 \times 9 = 90$$

$$11 \times 9 = 99$$

$$12 \times 9 = 108$$

Positive numbers are greater than zero

Negative numbers are less than zero

Directed numbers have a direction as well as a size.

Eg -7 , $+10$

We say $+5$ and -5 are reflections of each other as they are equal distance from the zero line.

Two things that are symmetrical are reflections of each other.

Ascending is when you order numbers from smallest to largest

Descending is when you order numbers from largest to smallest

Difference is the result of subtracting one number from another. E.g. the difference in -2 and 3 is 5

Increase means growing larger

Decrease means growing smaller

Zero pair are two numbers that combine to make zero. Eg 1 and -1
make 0

This button on a calculator changes the sign of a number.



Product - When you multiply two or more numbers the answer is the product.

e.g $5 \times 7 = 35$ 35 is the product.

To **partition** a number is to split into its component parts. Eg 6 is made from 5 and 1 .

Inverse operations are the opposite operation. Eg the inverse of adding is subtracting.

To **evaluate** an expression means to find a numerical value for it, to 'work it out'

To **simplify** an expression means to remove brackets, unnecessary terms and numbers

To **simplify** a fraction to its simplest form means to reduce the numerator and denominator in a fraction to the smallest numbers possible

Estimate is when you find an approximate answer to a calculation (normally by rounding numbers to 1 significant figure)

To **calculate** means you will have to do a sum either with or without a calculator.

Expression can contain letter and number terms along with symbols
e.g. $7 + 3$, $a^2 + 2b$

Equation is a statement showing two expressions are equal. The expressions are linked with a = sign
e.g. $7 - 2 = 4 + 1$, $5x = 10$

Solution is a value that can take place of a variable to make an equation true. e.g. $x + 5 = 7$, when we put x as 2 it makes the equation true

To **solve** is to find the solution of an equation

When we **balance** an equation we do the same operations on both sides of the equal sign.

Function Machine can input, applies a rule and delivers the answer as an output. We can use a function machine to solve an equation

Inverse operations are used to solve equations. Addition and subtraction, multiplication and division are inverse operations.

10^4 means 10 to the **power 4** which is $10 \times 10 \times 10 \times 10$.

The **Square** of a number is the product of the number with itself.
Eg the square of 5 is $5 \times 5 = 25$

Square root is a number whose square is equal to a given number. Eg square root of 25 is 5 because the square of 5 is 25.

$\sqrt{\quad}$ means square root. On a calculator the button is



Square and square root are the **inverse** of each other.

Cube is the result of multiplying to the power 3. Four cubed is $4 \times 4 \times 4 = 64$. This can be written as 4^3 .

The symbol $\sqrt{\quad}$ is called a **radical**.

Exponent is another word for index or power
Eg n^4 4 is the exponent

The **numerator** is the top number in a fraction. It tells us how many parts we have.

$$\frac{3}{5}$$

← numerator
← denominator

The **denominator** is the bottom number in a fraction. It shows how many parts the item has been split into.

Improper fractions have a numerator greater than the denominator.

Mixed fractions contain a whole number and a fraction.

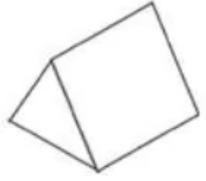
$$2\frac{1}{2} \rightarrow \frac{5}{2}$$

Mixed fraction Improper fraction

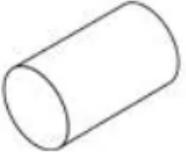
Equivalent fractions have the same value. Eg $\frac{3}{6} = \frac{1}{2} = \frac{5}{10}$

To add or subtract fractions the denominators must be the same. If they are not you will have to find equivalent fractions.

Triangular prism



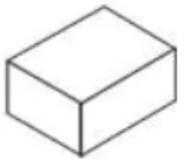
Cylinder



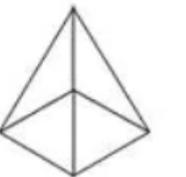
Cone



Cuboid



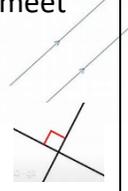
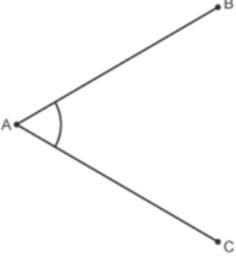
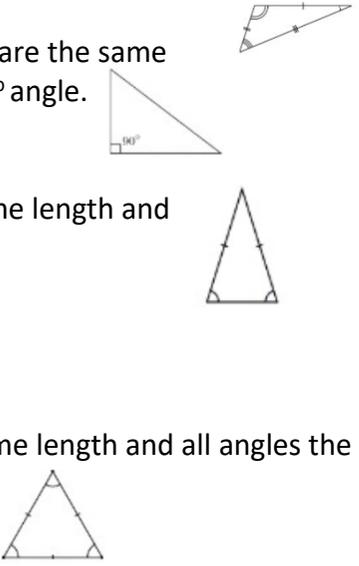
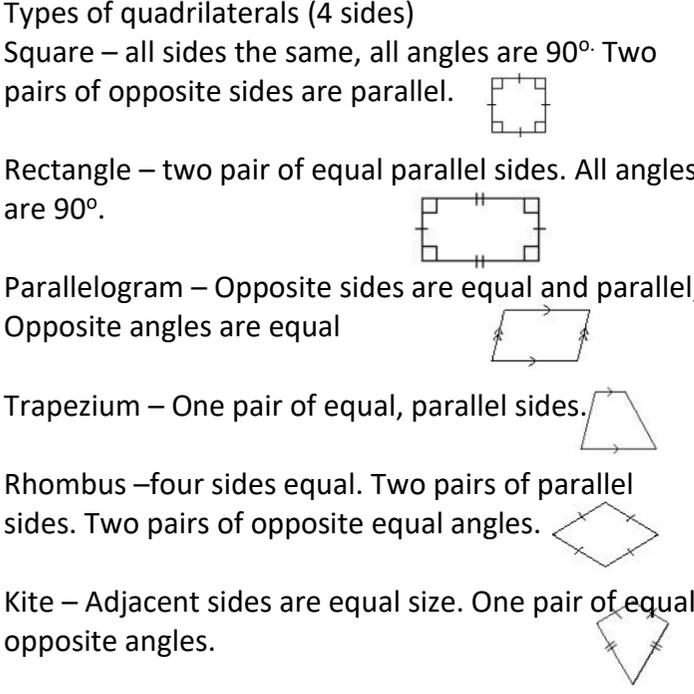
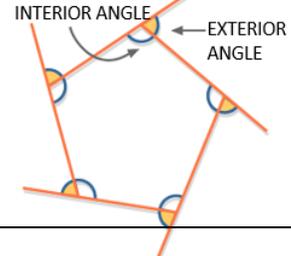
Square-based pyramid



Sphere



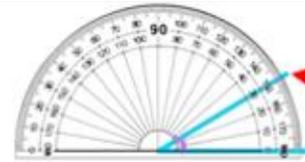
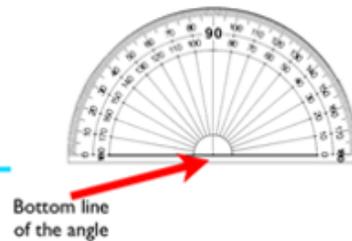
KNOWLEDGE ORGANISER: Year 7 Unit 10 – Constructing and Measuring

<p>Geometric terms: Line: a collection of points that go on forever on both directions Line Segment: part of a line that has two endpoints</p>	<p>Angle: Formed when two lines intersect (cross) Vertex: a corner of point where two lines meet</p>	<p>Parallel lines: lines that will never meet Perpendicular lines: Lines that intersect at 90°.</p> 																
<p>Labelling sides and angles Letters can be used to measure angles. AB and AC are line segments and they meet at point A. A is a vertex. AB joins the points A and B. The angle between AB and AC is labelled BAC. It can also be written as $\hat{B}AC$ or $\angle BAC$.</p> 		<p>Types of angles. Acute: Less than 90° Right: Exactly 90° (quarter turn) Obtuse: More than 90° but less than 180°. Straight line: Exactly 180° (half turn) Reflex: More than 180° but less than 360°. Full turn: Exactly 360°</p>																
<p>Types of triangles Scalene – no sides or angles are the same Right angled – contains a 90° angle. Isosceles – two sides the same length and two angles the same Equilateral – all sides the same length and all angles the same size</p> 	<p>Types of quadrilaterals (4 sides) Square – all sides the same, all angles are 90°. Two pairs of opposite sides are parallel. Rectangle – two pair of equal parallel sides. All angles are 90°. Parallelogram – Opposite sides are equal and parallel, Opposite angles are equal Trapezium – One pair of equal, parallel sides. Rhombus – four sides equal. Two pairs of parallel sides. Two pairs of opposite equal angles. Kite – Adjacent sides are equal size. One pair of equal opposite angles.</p> 	<p>Names of polygons: Regular polygons – all sides and interior angles are the same. Irregular polygons – sides and angles can be different sizes.</p> <table border="1" data-bbox="1590 901 2139 1220"> <tr> <td>3 sides</td> <td>Triangle</td> <td>7 sides</td> <td>Heptagon</td> </tr> <tr> <td>4 sides</td> <td>Quadrilateral</td> <td>8 sides</td> <td>Octagon</td> </tr> <tr> <td>5 sides</td> <td>Pentagon</td> <td>9 sides</td> <td>Nonagon</td> </tr> <tr> <td>6 sides</td> <td>Hexagon</td> <td>10 sides</td> <td>Decagon</td> </tr> </table> 	3 sides	Triangle	7 sides	Heptagon	4 sides	Quadrilateral	8 sides	Octagon	5 sides	Pentagon	9 sides	Nonagon	6 sides	Hexagon	10 sides	Decagon
3 sides	Triangle	7 sides	Heptagon															
4 sides	Quadrilateral	8 sides	Octagon															
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6 sides	Hexagon	10 sides	Decagon															

Measuring an angle

Rotate the protractor so the bottom line of the protractor matches with the bottom line.

Bottom line of the angle

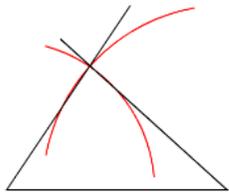


This is an acute angle so it reads 30°.

This is an obtuse angle so it reads 130°.



SSS – SIDE, SIDE, SIDE

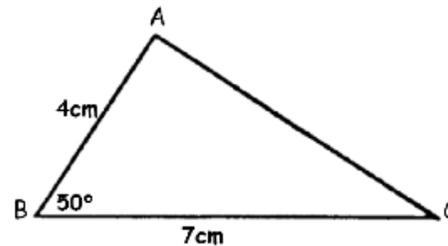


1. Draw the base of the triangle using a ruler.
2. Open a pair of compasses to the width of one side of the triangle.
3. Place the point on one end of the line and draw an arc.
4. Repeat for the other side of the triangle at the other end of the line.
5. Using a ruler, draw lines connecting the ends of the base of the triangle to the point where the arcs intersect.

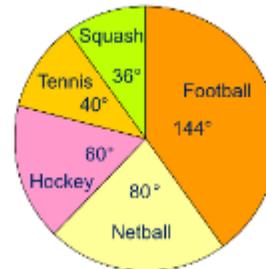
When drawing a pie chart, **divide 360° by the total frequency**. This will tell you how many degrees to use for the frequency of each category.

Remember to **label** the category that each sector in the pie chart represents.

SAS – SIDE ANGLE SIDE

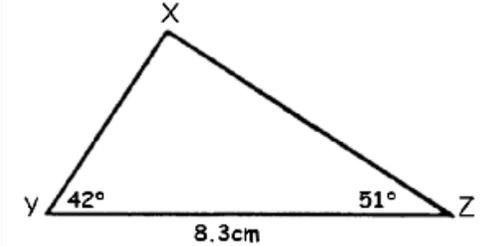


1. Draw the base of the triangle using a ruler.
2. Measure the angle required using a protractor and mark this angle.
3. Remove the protractor and draw a line of the exact length required in line with the angle mark drawn.
4. Connect the end of this line to the other end of the base of the triangle.



If there are 40 people in a survey, then each person will be worth $360 \div 40 = 9^\circ$ of the pie chart.

ASA – ANGLE SIDE ANGLE

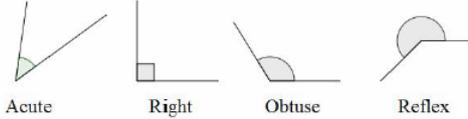
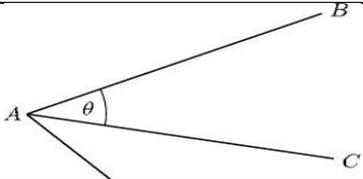
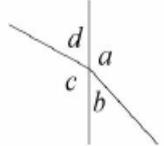
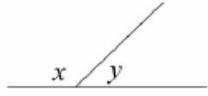
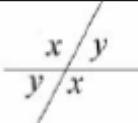
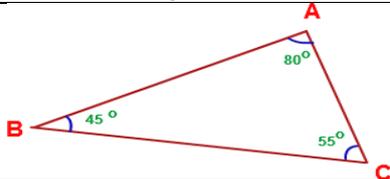
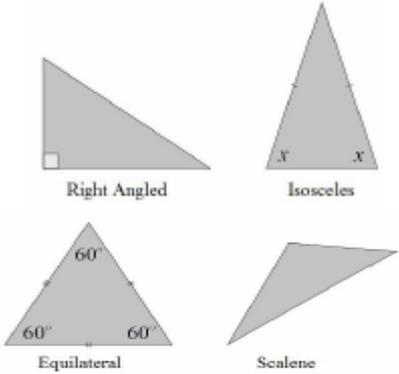
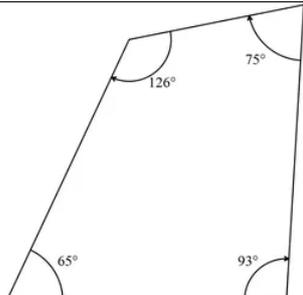


1. Draw the base of the triangle using a ruler.
2. Measure one of the angles required using a protractor and mark this angle.
3. Draw a straight line through this point from the same point on the base of the triangle.
4. Repeat this for the other angle on the other end of the base of the triangle.

You can write the proportion of each section by writing the angle as a fraction of 360.

$$\text{EG. Tennis is } \frac{40}{360} = \frac{1}{9}$$

If we knew there were 20 people who played tennis then we could work out the total frequency for the whole pie chart. If $\frac{1}{9} = 20$ then $20 \times 9 = 180$ gives the total frequency as 180 people

Topic/Skill	Definition/Tips	Example
1. Types of Angles	<p>Acute angles are less than 90°.</p> <p>Right angles are exactly 90°.</p> <p>Obtuse angles are greater than 90° but less than 180°.</p> <p>Reflex angles are greater than 180° but less than 360°.</p>	 <p>Acute Right Obtuse Reflex</p>
2. Angle Notation	<p>Can use one lower-case letters, eg. θ or x</p> <p>Can use three upper-case letters, eg. BAC</p>	
3. Angles at a Point	Angles around a point add up to 360°.	 <p>$a + b + c + d = 360^\circ$</p>
4. Angles on a Straight Line	Angles around a point on a straight line add up to 180°.	 <p>$x + y = 180^\circ$</p>
5. Opposite Angles	Vertically opposite angles are equal.	
6. Angles in a Triangle	Angles in a triangle add up to 180°.	
7. Types of Triangles	<p>Right Angle Triangles have a 90° angle in.</p> <p>Isosceles Triangles have 2 equal sides and 2 equal base angles.</p> <p>Equilateral Triangles have 3 equal sides and 3 equal angles (60°).</p> <p>Scalene Triangles have different sides and different angles.</p> <p>Base angles in an isosceles triangle are equal.</p>	 <p>Right Angled Isosceles</p> <p>Equilateral Scalene</p>
8. Angles in a Quadrilateral	Angles in a quadrilateral add up to 360°.	

12 times tables

$1 \times 12 = 12$

$2 \times 12 = 24$

$3 \times 12 = 36$

$4 \times 12 = 48$

$5 \times 12 = 60$

$6 \times 12 = 72$

$7 \times 12 = 84$

$8 \times 12 = 96$

$9 \times 12 = 108$

$10 \times 12 = 120$

$11 \times 12 = 132$

$12 \times 12 = 144$

To find the **fraction** of a given amount

- 1) Divide the amount by the denominator
- 2) Multiply the result by the numerator

A **Percentage** is a rate, number, or amount in each hundred.

Percent means per 100

A **fraction** is a numerical quantity that is not a whole number

Whole means entire or all

The **original** means present or existing from the beginning; the first or earliest.

Place Value is the numerical value that a digit has because of its position in a number.

A **decimal** is a system of numbers and arithmetic based on the number ten, tenth parts, and powers of.

- To find **50%** you divide the 100% value by 2.
 To find **10%** you divide the 100% value by 10.
 To find **20%** you divide the 100% value by 5.
 To find **25%** you divide the 100% value by 4.
 To find **1%** you divide the 100% value by 100.

Line: a collection of points that go on forever on both directions.

Line Segment: part of a line that has two endpoints.

Angle: Formed when two lines intersect (cross)

Vertex: a corner of point where two lines meet.

Parallel lines: lines that will never meet.



Perpendicular lines: Lines that intersect at 90°.



Measuring an angle

Rotate the protractor so the bottom line of the protractor matches with the bottom line.

Bottom line of the angle

Bottom line of the angle



This is an acute angle so it reads 30°.

This is an obtuse angle so it reads 130°.

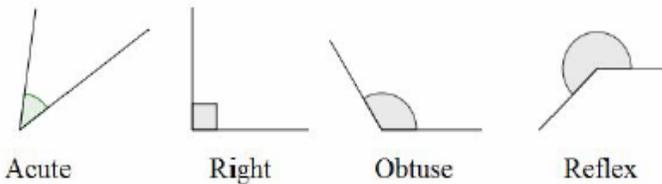


Acute angles are less than 90° .

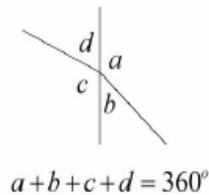
Right angles are exactly 90° .

Obtuse angles are greater than 90° but less than 180° .

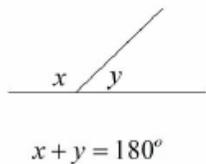
Reflex angles are greater than 180° but less than 360° .



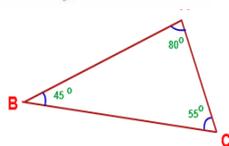
Angles around a **point** add up to 360° .



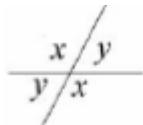
Angles on a **straight line** add up to 180° .



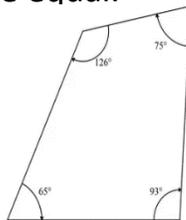
Angles in a **triangle** add up to 180° .



Vertically opposite angles are equal.



Angles in a **quadrilateral** add up to 360° .



Types of triangles

Scalene – no sides or angles are the same

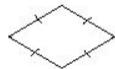
Right angled – contains a 90° angle.

Isosceles – two sides the same length and two angles the same

Equilateral – all sides the same length and all angles the same size.

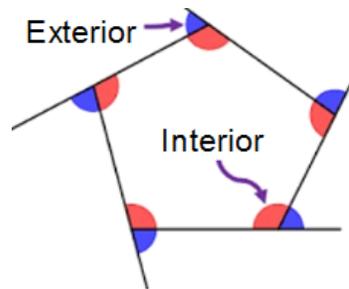
Names of polygons:

Regular polygons – all sides and angles are the same.



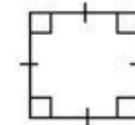
Irregular polygons – sides and angles can be different sizes.

- 3 sides Triangle
- 4 sides Quadrilateral
- 5 sides Pentagon
- 6 sides Hexagon
- 7 sides Heptagon
- 8 sides Octagon
- 9 sides Nonagon
- 10 sides Decagon



Types of **quadrilaterals** (4 sides)

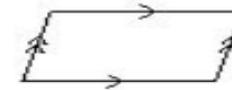
Square – all sides the same, all angles are 90° . Two pairs of opposite sides are parallel.



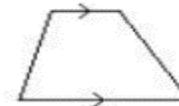
Rectangle – two pairs of equal parallel sides. All angles are 90° .



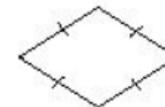
Parallelogram – Opposite sides are equal and parallel, Opposite angles are equal



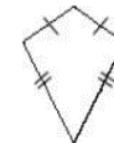
Trapezium – One pair of equal, parallel sides.



Rhombus – four sides equal. Two pairs of parallel sides. Two pairs of opposite equal angles.



Kite – Adjacent sides are equal size. One pair of equal opposite angles.



- $\frac{1}{100} = 0.01 = 1\%$
- $\frac{1}{20} = 0.05 = 5\%$
- $\frac{1}{10} = 0.1 = 10\%$
- $\frac{1}{5} = 0.2 = 20\%$
- $\frac{1}{4} = 0.25 = 25\%$
- $\frac{1}{3} = 0.3 = 33.3\%$
- $\frac{1}{2} = 0.5 = 50\%$
- $\frac{2}{3} = 0.6 = 66.7\%$
- $\frac{3}{4} = 0.75 = 75\%$
- $1 = 100\%$

- 10mm = 1cm
- 100cm = 1m
- 1000m = 1km

1000g = 1kg

1000ml = 1 litre

YEAR 7 — REASONING WITH NUMBER

Developing number sense

@whisto_maths

What do I need to be able to do?

By the end of this unit you should be able to:

- Know and use mental addition/ subtraction
- Know and use mental multiplication/ division
- Know and use mental arithmetic for decimals
- Know and use mental arithmetic for fractions
- Use factors to simplify calculations
- Use estimation to check mental calculations
- Use number facts
- Use algebraic facts

Keywords

- Commutative:** changing the order of the operations does not change the result
- Associative:** when you add or multiply you can do so regardless of how the numbers are grouped
- Dividend:** the number being divided
- Divisor:** the number we divide by
- Expression:** a maths sentence with a minimum of two numbers and at least one math operation (no equals sign)
- Equation:** a mathematical statement that two things are equal
- Quotient:** the result of a division

Mental methods for addition/ subtraction

Addition is commutative



$$6 + 3 = 3 + 6$$

The order of addition does not change the result

Subtraction the order has to stay the same

$$360 - 147 = 360 - 100 - 40 - 7$$

- Number lines help for addition and subtraction
- Working in 10's first aids mental addition/ subtraction

Mental methods for multiplication/ division

Multiplication is commutative



$$2 \times 4 = 4 \times 2$$

The order of multiplication does not change the result

Partitioning can help multiplication

$$\begin{aligned} 24 \times 6 &= 20 \times 6 + 4 \times 6 \\ &= 120 + 24 \\ &= 144 \end{aligned}$$

Division is not associative

Chunking the division can help $4000 \div 25$
"How many 25's in 100" then how many chunks of that in 4000.

Mental methods for decimals

Multiplying by a decimal < 1 will make the original value smaller e.g. $0.1 = \div 10$

Methods for multiplication 12×0.03

$$\begin{array}{l} 12 \times 3 = 36 \\ 12 \times 3 = 36 \\ 12 \times 0.3 = 3.6 \\ 12 \times 0.03 = 0.36 \end{array} \quad \begin{array}{l} 12 \times 3 = 36 \\ +10 \downarrow +100 \downarrow +1000 \downarrow \\ 12 \times 0.03 = 0.36 \end{array}$$

Methods for division $15 \div 0.05$

Multiply by powers of 10 until the divisor becomes an integer

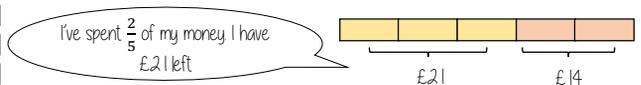
$$\begin{array}{l} 1.5 \div 0.05 \\ \times 100 \downarrow \quad \times 100 \downarrow \\ 150 \div 5 = 30 \end{array}$$

Methods for addition $2.3 + 2.4$

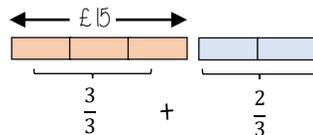
$$\begin{array}{l} 2 + 2 = 4 \\ 0.3 + 0.4 = 0.7 \\ 4 + 0.7 = 4.7 \end{array}$$

Mental methods for fractions

Use bar models where possible



How much did they have to begin with?



What is $\frac{5}{3}$ of £15?

Using factors to simplify calculations

$$30 \times 16$$

$$10 \times 3 \times 4 \times 4$$

$$10 \times 3 \times 2 \times 8$$

$$2 \times 5 \times 3 \times 2 \times 2 \times 2 \times 2$$

$$16 \times 10 \times 3$$

Multiplication is commutative
Factors can be multiplied in any order

Estimation

Estimations are useful — especially when using fractions and decimals to check if your solution is possible.

Most estimations round to 1 significant figure

Estimations are useful — especially when using fractions and decimals to check if your solution is possible.

$$210 + 899 < 1200$$

This is true because even if both numbers were rounded up, they would reach $300 + 900$.

The correct estimation would be $200 + 900 = 1100$.

Number facts

Use $124 \times 5 = 620$

For multiplication, each value that is multiplied or divided by powers of 10 needs to happen to the result

$$620 \div 124 = 50$$

For division you must consider the impact of the divisor becoming smaller or bigger.
Smaller — the answer will be bigger (it is being shared into less parts)
Bigger — the answer will be smaller (it is being shared into more parts)

Algebraic facts

$$2a + 2b = 10 \quad \text{Everything } \times 2$$

$$0.1a + 0.1b = 0.5$$

Everything $\div 10$

$$a + b = 5$$

Add 2 to the total

$$a + b + 2 = 7$$

The unknown quantity isn't changing but the variables change what is done to give the result

YEAR 7 — REASONING WITH NUMBER

Sets and probability

@whisto_maths

What do I need to be able to do?

By the end of this unit you should be able to:

- Identify and represent sets
- Interpret and create Venn diagrams
- Understand and use the intersection of sets
- Understand and use the union of sets
- Generate sample spaces for single events
- Calculate the probability of a single event
- Understand and use the probability scale

Keywords

Set: collection of things
Element: each item in a set is called an element
Intersection: the overlapping part of a Venn diagram ($A \cap B$)
Union: two ellipses that join ($A \cup B$)
Mutually Exclusive: events that do not occur at the same time
Probability: likelihood of an event happening
Bias: a built-in error that makes all values wrong (unequal) by a certain amount, e.g. a weighted dice
Fair: there is zero bias, and all outcomes have an equal likelihood
Random: something happens by chance and is unable to be predicted

Identify and represent sets

The **universal set** has this symbol ξ — this means **EVERYTHING** in the Venn diagram is in this set

A set is a collection of things — you write sets inside curly brackets { }

$\xi = \{\text{the numbers between 1 and 50 inclusive}\}$

My sets can include every number between 1 and 50 including those numbers

$A = \{\text{Square numbers}\}$
 $A = \{1, 4, 9, 16, 25, 36, 49\}$

All the numbers in set A are square number and between 1 and 50

Interpret and create Venn diagrams

Mutually exclusive sets
 The two sets have nothing in common
 No overlap

Union of sets
 The two sets have some elements in common — they are placed in the intersection

Subset
 All of set B is also in Set A so the ellipse fits inside the set

The box
 Around the outside of every Venn diagram will be a box. If an element is not part of any set it is placed outside an ellipse but inside the box

Intersection of sets

Elements in the intersection are in set A AND set B

The notation for this is $A \cap B$

$\xi = \{\text{the numbers between 1 and 15 inclusive}\}$
 $A = \{\text{Multiples of 5}\}$ $B = \{\text{Multiples of 3}\}$

The element in $A \cap B$ is 15

In this example there is only one number that is both a multiple of 3 and a multiple of 5 between 1 and 15

Union of sets

Elements in the union could be in set A OR set B

The notation for this is $A \cup B$

There are 7 elements that are either a multiple of 5 OR a multiple of 3 between 1 and 15

This Venn shows the **number of elements** in each set

Sample space — for single events

A sample space represents a possible outcome from an event

They can be interpreted in a variety of ways because they do not tell you the probability

A sample space for rolling a six-sided dice is $S = \{1, 2, 3, 4, 5, 6\}$

A sample space for this spinner is $S = \{\text{Pink, Blue, Yellow}\}$

You only need to write each element once in a sample space diagram

Probability of a single event

Probability = $\frac{\text{number of times event happens}}{\text{total number of possible outcomes}}$

$P(\text{Blue}) = \frac{4}{10}$ ← There are 4 blue sectors
 ← There are 10 sectors overall

Probability notation $P(\text{event}) = \frac{2}{5}$

Probability can be a fraction, decimal or percentage value

$\frac{4}{10} = \frac{40}{100} = 0.40 = 40\%$

Probability is always a value between 0 and 1

The probability scale

Impossible 0 or 0% Even chance 0.5, $\frac{1}{2}$ or 50% Certain 1 or 100%

The more likely an event the further up the probability it will be in comparison to another event (It will have a probability closer to 1)

There are 2 pink and 2 yellow balls, so they have the same probability

There are 5 possible outcomes So 5 intervals on this scale, each interval value is $\frac{1}{5}$

Sum of probabilities

Probability is always a value between 0 and 1

The probability of getting a blue ball is $\frac{1}{5}$
 ∴ The probability of **NOT** getting a blue ball is $\frac{4}{5}$

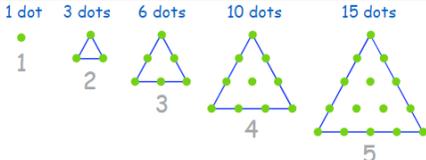
The sum of the probabilities is 1

The table shows the probability of selecting a type of chocolate

Dark	Milk	White
0.15	0.35	

$P(\text{white chocolate}) = 1 - 0.15 - 0.35 = 0.5$

KNOWLEDGE ORGANISER: Year 7 Unit 14 – Prime Numbers and Proof

Name	Definition	Example	Non-example
Divisible	When an amount can be divided by a specified number	120 is divisible by 5 (=24)	204 is not divisible by 100
Divisor	The number we are dividing by	The divisor in the calculation $63 \div 9 = 7$ is 9	
Factorise	Take out the common factors in an expression (to write the expression using brackets)	Factorising $2y+6 = 2(y+3)$	
Product	The result of multiplying 2 or more terms together	The product of $3a$ and $5b$ is $15ab$	
Highest Common Factor (HCF)	The largest number that can divide 2 or more given numbers	The HCF of 10, 15 and 50 is 5	The HCF of 6 and 8 is not 3
Lowest Common Multiple (LCM)	The lowest number that would appear the times tables of 2 or more given numbers	The LCM of 3, 8 and 10 is 120	
Prime number	A number that has exactly two factors, itself and one.	2, 3, 5, 7, 11, 13, 17, 19, 23, 29...	1 (only has 1 factor) Anything in the 2 times table (except 2)
Square numbers	The result of multiplying a number by itself	1, 4, 9, 16, 25, 36, 49, 64, 81, 100, 121, 144, 169, 196, 225...	
Triangle numbers	A number that can make a triangular dot pattern	 <p>1 dot 3 dots 6 dots 10 dots 15 dots</p>	
Express	Write the terms in a certain way	27 expressed as a product of prime numbers is $3 \times 3 \times 3 = 3^3$	
Conjecture	A statement that could be true or false, is yet to be proved	"To find the area of a shape, multiply length by width"	
Counterexample	An example that proves another statement false	The area is found by multiplying the length by the width. A counterexample to this is the area of a triangle is $\text{base} \times \text{height} \div 2$	
Proof	Logical mathematical arguments used to show the truth of a mathematical statement		

25 times tables

$1 \times 25 = 25$

$2 \times 25 = 50$

$3 \times 25 = 75$

$4 \times 25 = 100$

$5 \times 25 = 125$

$6 \times 25 = 150$

$7 \times 25 = 175$

$8 \times 25 = 200$

$9 \times 25 = 225$

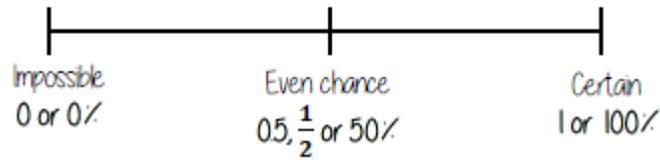
$10 \times 25 = 250$

$11 \times 25 = 275$

$12 \times 25 = 300$

Probability is the likelihood of an event happening.

Probability can be measured on a **scale**.



The more **likely** an event the further up the probability it will be in comparison to another event. (It will have a probability closer to 1)

Probability is always a value between 0 and 1.

Probability can be a fraction, decimal or percentage value. (never write as a ratio)

P(A) refers to the probability that event A will occur.

$$\text{Probability} = \frac{\text{number of times an event happens}}{\text{total number of possible outcomes}}$$

A **sample space** represents the **set of all possible outcomes** of an experiment.

A sample space for rolling a six-sided dice is $S = \{1, 2, 3, 4, 5, 6\}$.

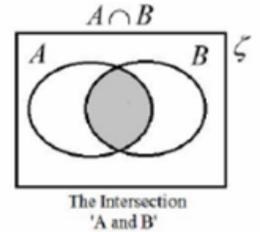
A **Venn diagram** is a diagram using circles or other shapes, to show the relationship between sets.

Set: collection of things. You write sets inside curly brackets { }.

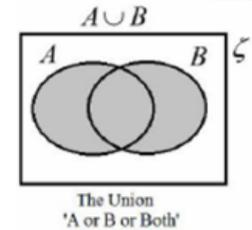
Element: each item in a set is called an element.

The **universal set** has this symbol ξ this means EVERYTHING in the Venn diagram is in this set.

Intersection: the overlapping part of a Venn diagram (AND \cap).



Union: two ellipses that join (OR \cup).



Mutually Exclusive: events that do not occur at the same time.

Bias: a built-in error that makes all values wrong (unequal) by a certain amount, e.g. a weighted dice.

Fair: there is zero bias, and all outcomes have an equal likelihood.

Random: something happens by chance and is unable to be predicted.

Associative means we can complete the calculation in any order $(4 + 7) + 1 = 4 + (7 + 1)$
 $11 + 1 = 4 + 8$

Commutative:

Adding is commutative because $2 + 7 = 9$ and $7 + 2 = 9$

It doesn't matter which way round you add
Subtracting is not commutative because $5 - 2 = 3$ but $2 - 5 = -3$

Multiples of a number are found by multiplying that number by an integer.

When a number can be written as a product of two numbers, these are **factors**.

You can use factors to simplify calculations e.g. $18 \times 30 = (9 \times 2) \times (10 \times 3)$
 $= 9 \times 3 \times 2 \times 10 = 540$.

Perform the calculations by multiplying the factors in the easiest order.

Most estimations mean you have to round numbers to 1 significant figure.

For division you must consider the impact of the **divisor** becoming smaller or bigger.
Smaller – the answer will be bigger.
Bigger – the answer will be smaller.

Prime number

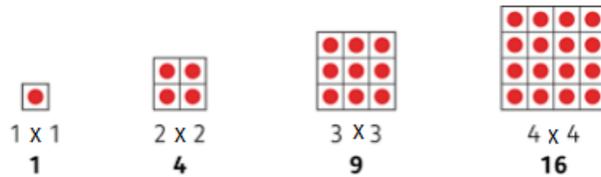
A number that has exactly two factors, itself and one.

Prime numbers to 50 are:

2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47.

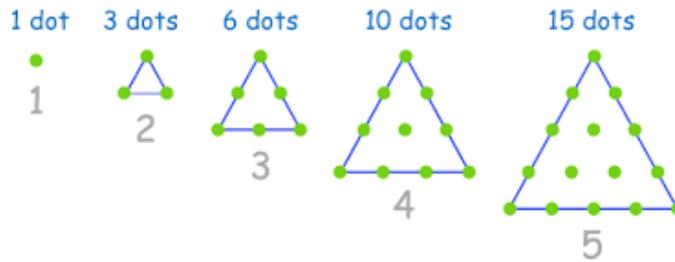
Square numbers

The result of multiplying a number by itself.
The first 10 square numbers are: 1, 4, 9, 16, 25, 36, 49, 64, 81, 100.



Triangle numbers

A number that can make a triangular dot pattern. Each row is 1 more than the last row.



Two consecutive triangle numbers add to make a square number.

Lowest common multiple

The smallest number that is a multiple of two numbers e.g. **LCM** of 20 and 12 is 60.

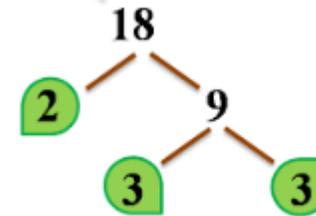
Highest common factor

The largest number that is a factor of two numbers e.g. **HCF** of 20, and 12 is 4.

Prime factor decomposition

A number broken down into a multiplication sum that only uses primes e.g. $12 = 2 \times 2 \times 3$ e.g. $18 = 2 \times 3 \times 3$

You can use a **prime factor tree** to help find the prime factors



A **counter example** is an example that proves another statement false

A **conjecture** is a statement that could be true or false, is yet to be proved.

A **proof** is a logical mathematical argument used to show the truth of a mathematical statement.



- 1 minute = 60 seconds
- 1 hour = 60 minutes
- 1 day = 24 hours
- 1 week = 7 days
- 52 weeks = 1 year
- 12 months = 1 year
- 365 days = 1 year (366 in a leap year)
- A leap year every 4 years



- 52 cards in a pack
- 4 suits in a pack
- 13 Spades (black)
- 13 Clubs (black)
- 13 Hearts (red)
- 13 Diamonds (red)

Suits contain:
Ace, 2, 3, 4, 5, 6, 7, 8, 9, 10, Jack, Queen, King

