

Write your name here

Surname <b>WORKED SOLUTIONS</b>	Other names
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**Pearson Edexcel** Centre Number 

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 Candidate Number 

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**Level 1/Level 2 GCSE (9-1)**


**Mathematics**

**Paper 3 (Calculator)**

**Higher Tier**

Tuesday 12 June 2018 – Morning <b>Time: 1 hour 30 minutes</b>	Paper Reference <b>1MA1/3H</b>
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**You must have:** Ruler graduated in centimetres and millimetres, protractor, pair of compasses, pen, HB pencil, eraser, calculator. Tracing paper may be used.

Total Marks 

### Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You must **show all your working**.
- Diagrams are **NOT** accurately drawn, unless otherwise indicated.
- **Calculators may be used.**
- If your calculator does not have a  $\pi$  button, take the value of  $\pi$  to be 3.142 unless the question instructs otherwise.



### Information

- The total mark for this paper is 80
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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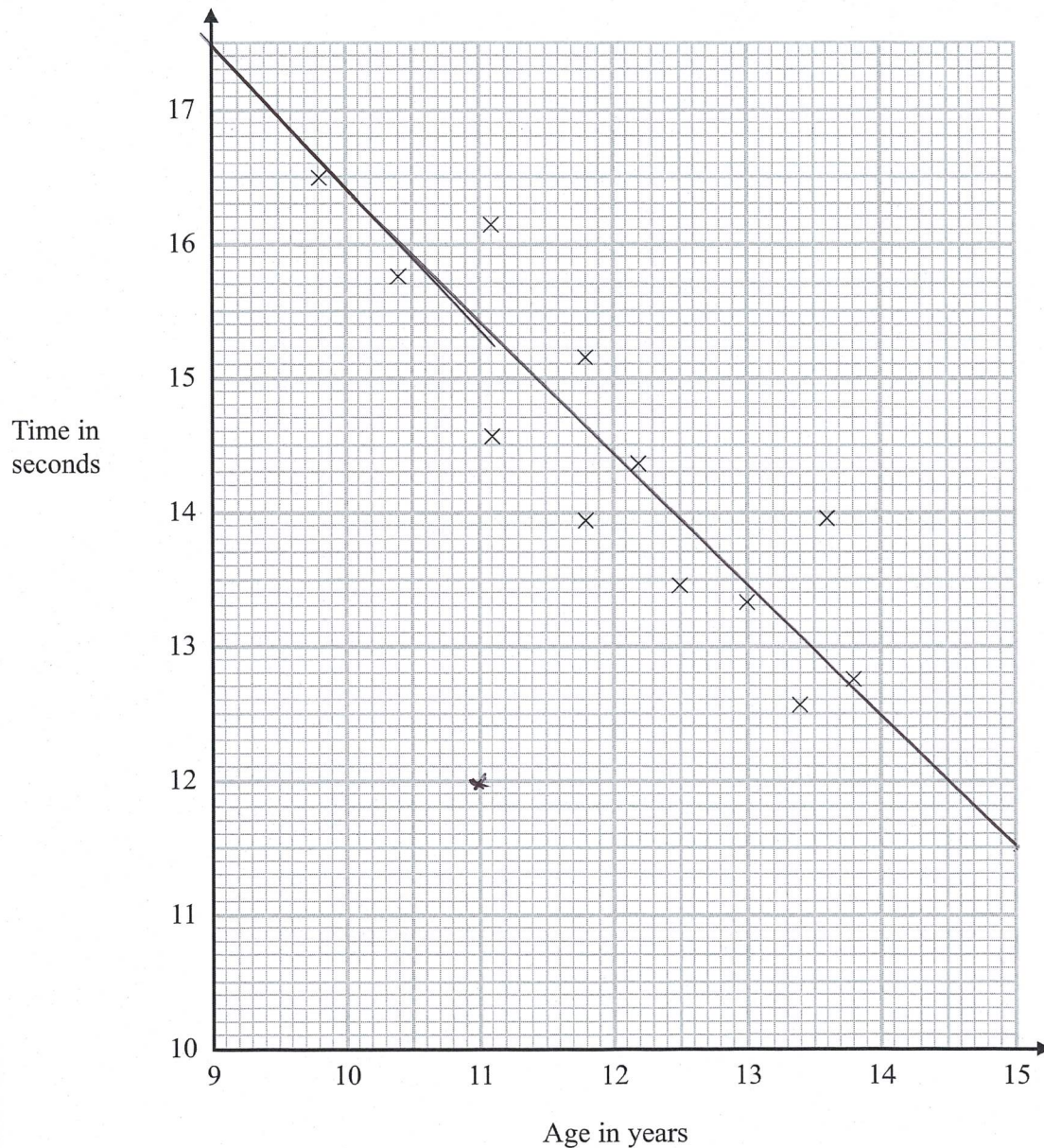
Answer ALL questions.

Write your answers in the spaces provided.

You must write down all the stages in your working.

- 1 The scatter diagram shows information about 12 girls.

It shows the age of each girl and the best time she takes to run 100 metres.



- (a) Write down the type of correlation.

Negative

(1)





Kristina is 11 years old.

Her best time to run 100 metres is 12 seconds.

The point representing this information would be an outlier on the scatter diagram.

(b) Explain why.

It is away from all the other points - it does not follow the trend

(1)

Debbie is 15 years old.

Debbie says,

"The scatter diagram shows I should take less than 12 seconds to run 100 metres."

(c) Comment on what Debbie says.

The point would be outside the range of data, so unreliable.

(1)

(Total for Question 1 is 3 marks)

2 Expand and simplify  $5(p + 3) - 2(1 - 2p)$

$$5p + 15 - 2 + 4p$$

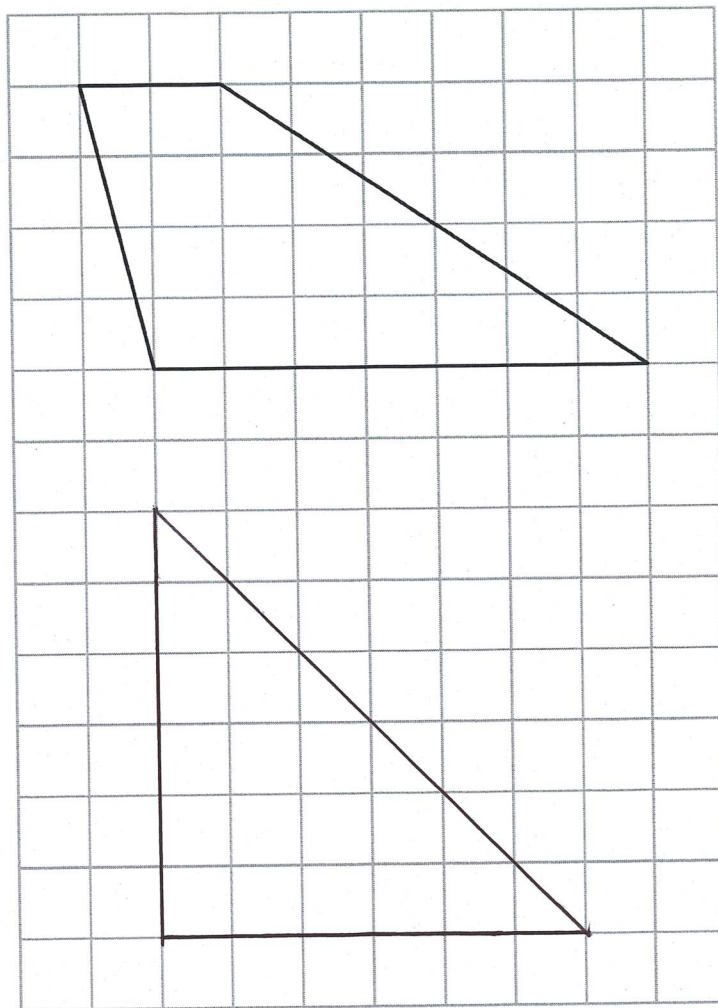
$$9p + 13$$

$$9p + 13$$

(Total for Question 2 is 2 marks)



- 3 Here is a trapezium drawn on a centimetre grid.



On the grid, draw a triangle equal in area to this trapezium.

$$\begin{aligned}\text{Area} &= \frac{(7+2)4}{2} \\ &= \frac{9 \times 4}{2} \\ &= 18\end{aligned}$$

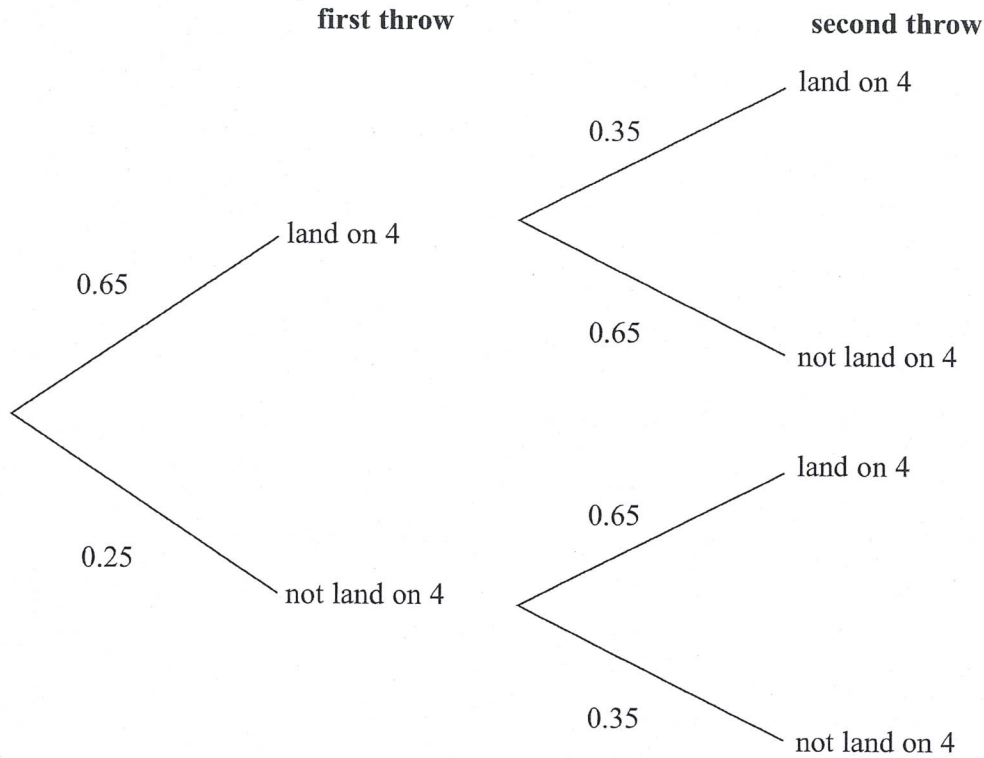
(Total for Question 3 is 2 marks)





- 4 When a biased 6-sided dice is thrown once, the probability that it will land on 4 is 0.65. The biased dice is thrown twice.

Amir draws this probability tree diagram.  
The diagram is **not** correct.



Write down **two** things that are wrong with the probability tree diagram.

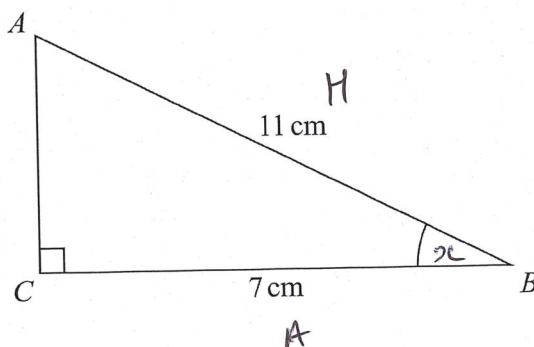
1 The first throw probabilities do not add to 1

2 The probability 0.65 changes from land on 4 to not land on 4 on the same dice

(Total for Question 4 is 2 marks)



- 5  $ABC$  is a right-angled triangle.



- (a) Work out the size of angle  $ABC$ .  
Give your answer correct to 1 decimal place.

$$\cos x = \frac{A}{H}$$

$$\cos x = \frac{7}{11}$$

$$x = 50.478$$

$$x = 50.5$$

$$\underline{50.5}^{\circ}$$

(2)

The length of the side  $AB$  is reduced by 1 cm.

The length of the side  $BC$  is still 7 cm.  
Angle  $ACB$  is still  $90^{\circ}$

- (b) Will the value of  $\cos ABC$  increase or decrease?  
You must give a reason for your answer.

Increase as  $\frac{7}{10}$  is greater than  $\frac{7}{11}$

(1)

(Total for Question 5 is 3 marks)





- 6 There are some counters in a bag.  
The counters are red or white or blue or yellow.

Bob is going to take at random a counter from the bag.

The table shows each of the probabilities that the counter will be blue or will be yellow.

Colour	red	white	blue	yellow
Probability	$2x$ $0.2$	$x$ $0.1$	0.45	0.25

There are 18 blue counters in the bag.

The probability that the counter Bob takes will be red is twice the probability that the counter will be white.

- (a) Work out the number of red counters in the bag.

$$\begin{aligned}
 2x + x + 0.45 + 0.25 &= 1 \\
 3x + 0.7 &= 1 \\
 3x &= 0.3 \\
 x &= 0.1
 \end{aligned}$$

Blue

$$\frac{18}{\text{total}} = 0.45$$

$$\frac{18}{0.45} = \text{total}$$

$$40 = \text{total}$$

Red

$$0.2 \times 40 = 8$$

8

(4)

A marble is going to be taken at random from a box of marbles.  
The probability that the marble will be silver is 0.5

There must be an even number of marbles in the box.

- (b) Explain why.

$0.5 = \text{half}$ , so you must be able to half the amount  
so therefore it must be even.

(1)

(Total for Question 6 is 5 marks)



7 Solve  $\frac{5-x}{2} = 2x-7$

$$5-x = 4x-14$$

$$19 = 5x$$

$$3.8 = \frac{19}{5} = x$$

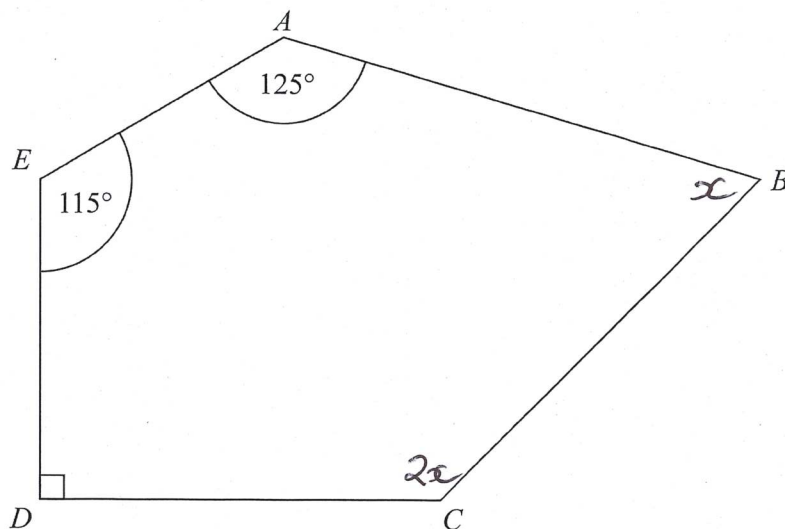
$$x = 3.8$$

(Total for Question 7 is 3 marks)





8  $ABCDE$  is a pentagon.



Angle  $BCD = 2 \times$  angle  $ABC$

Work out the size of angle  $BCD$ .  
You must show all your working.

$$\begin{aligned} \text{Total angles} &= (5-2) \times 180 \\ &= 540 \end{aligned}$$

So

$$90 + 115 + 125 + x + 2x = 540$$

$$330 + 3x = 540$$

$$3x = 210$$

$$x = 70$$

$$BCD = 140$$

140

(Total for Question 8 is 5 marks)



P 4 8 8 6 4 A 0 9 2 4

9  $T = \sqrt{\frac{w}{d^3}}$

$w = 5.6 \times 10^{-5}$

$d = 1.4 \times 10^{-4}$

(a) Work out the value of  $T$ .

Give your answer in standard form correct to 3 significant figures.

$$\begin{aligned} & 4517.539515 \\ & = 4520 \\ & = 4.52 \times 10^3 \end{aligned}$$

$$T = 4.52 \times 10^3 \quad (2)$$

$w$  is increased by 10%

$d$  is increased by 5%

Lottie says,

"The value of  $T$  will increase because both  $w$  and  $d$  are increased."

(b) Lottie is wrong.

Explain why.

$$\begin{aligned} T &= \sqrt{\frac{w \times 1.1}{(d \times 1.05)^3}} \\ &= 4403.6658 \\ &= 4400 \\ &= 4.4 \times 10^3 \end{aligned}$$

$$4.4 < 4.52$$

So decreased

OR

$$\begin{aligned} SF &= \sqrt{\frac{1.1}{1.05^3}} \\ &= 0.97 \end{aligned}$$

$$0.97 < 1$$

So decreased.

(2)

(Total for Question 9 is 4 marks)





10 Here are three lamps.

lamp A



lamp B



lamp C



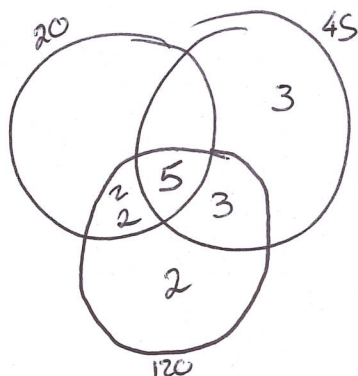
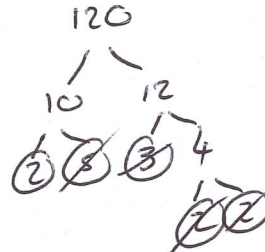
Lamp A flashes every 20 seconds.

Lamp B flashes every 45 seconds.

Lamp C flashes every 120 seconds.

The three lamps start flashing at the same time.

How many times in one hour will the three lamps flash at the same time?



$$\begin{aligned} \text{LCM} &= 2^3 \times 3^2 \times 5 \\ &= 360 \text{ sec} \\ &= 6 \text{ min} \end{aligned}$$

$$1\text{h} = 60\text{min}$$

$$60 \div 6 = 10$$

10

(Total for Question 10 is 3 marks)



DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

11 In 2003, Jerry bought a house.

In 2007, Jerry sold the house to Mia.  
He made a profit of 20% 1.2

In 2012, Mia sold the house for £162 000  
She made a loss of 10%

0.9  
Work out how much Jerry paid for the house in 2003

$$\frac{\text{Mia paid}}{0.9} = \frac{162000}{0.9} = \pounds 180000$$

$$\frac{\text{Jerry paid}}{1.2} = \frac{180000}{1.2} = \pounds 150000$$

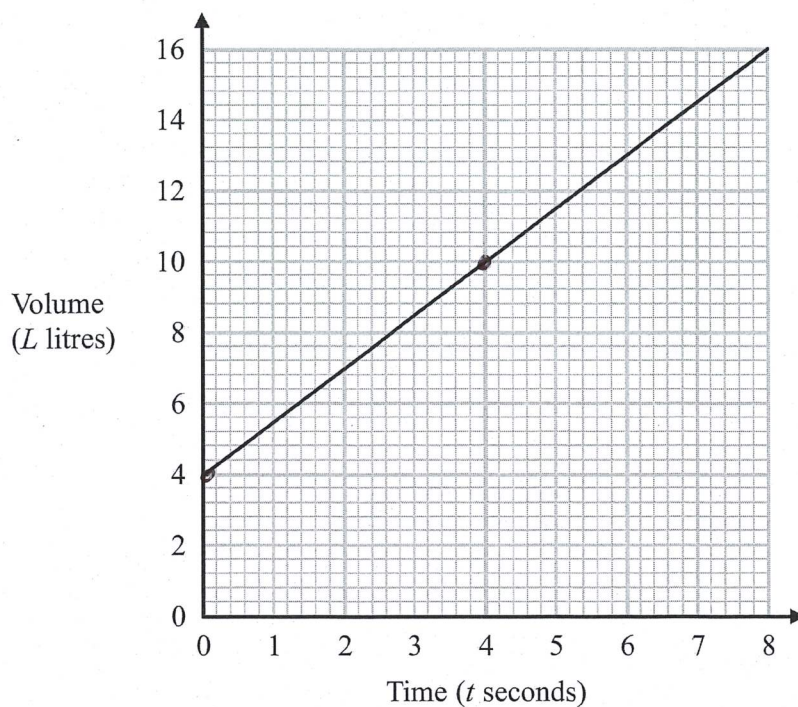
£ 150 000

(Total for Question 11 is 3 marks)





12 The graph shows the volume of liquid ( $L$  litres) in a container at time  $t$  seconds.



(a) Find the gradient of the graph.

$$\frac{10-4}{4-0} = \frac{6}{4} = 1.5$$

1.5

(2)

(b) Explain what this gradient represents.

Rate of change of volume over time

(1)

The graph intersects the volume axis at  $L = 4$

(c) Explain what this intercept represents.

The container starts with 4L already in.

(1)

(Total for Question 12 is 4 marks)



13 Here are two similar solid shapes.



surface area of shape A : surface area of shape B = 3 : 4

The volume of shape B is  $10 \text{ cm}^3$

Work out the volume of shape A.

Give your answer correct to 3 significant figures.

$$\begin{array}{l} L : \sqrt{3} : 2 \\ A : 3 : 4 \\ V : \sqrt{3^3} : 8 \\ \quad = \sqrt{27} : 8 \end{array} \quad \left. \begin{array}{l} \nearrow \\ \searrow \end{array} \right\}^3$$

$$\frac{\sqrt{27}}{8} \times 10 = 6.49519$$

$$= 6.50$$

6.50 .....  $\text{cm}^3$

(Total for Question 13 is 3 marks)



DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

- 14 There are 16 hockey teams in a league.  
Each team played two matches against each of the other teams.

Work out the total number of matches played.

$$\frac{16 \times 30}{2} = 240$$

240

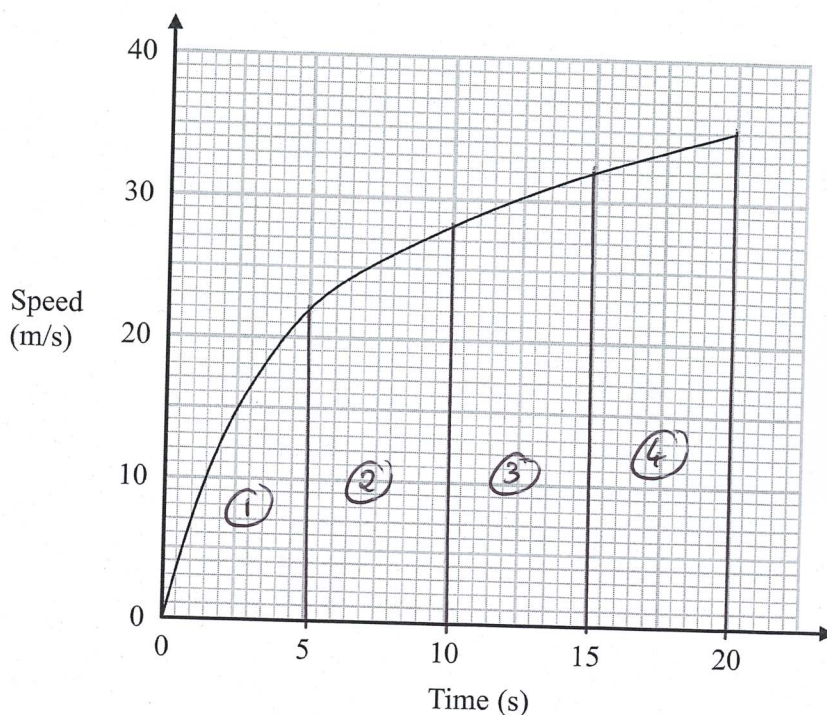
(Total for Question 14 is 2 marks)



P 4 8 8 6 4 A 0 1 5 2 4



- 15 The graph shows the speed of a car, in metres per second, during the first 20 seconds of a journey.



- (a) Work out an estimate for the distance the car travelled in the first 20 seconds. Use 4 strips of equal width.

Distance = Area under curve

$$\textcircled{1} \quad \frac{5 \times 22}{2} = 55$$

$$55 + 125 + 150 + 167.5$$

$$\textcircled{2} \quad \frac{(22 + 28) \times 5}{2} = \frac{50 \times 5}{2} = 125$$

$$= 497.5$$

$$\textcircled{3} \quad \frac{(28 + 32) \times 5}{2} = \frac{60 \times 5}{2} = 150$$

$$\textcircled{4} \quad \frac{(32 + 35) \times 5}{2} = \frac{67 \times 5}{2} = 167.5$$

..... metres

(3)



- (b) Is your answer to part (a) an underestimate or an overestimate of the actual distance the car travelled in the first 20 seconds?  
Give a reason for your answer.

Underestimation, as the curve goes above the straight  
lines used to make the triangles and trapezium

(1)

(Total for Question 15 is 4 marks)



P 4 8 8 6 4 A 0 1 7 2 4

16 The  $n$ th term of a sequence is given by  $an^2 + bn$  where  $a$  and  $b$  are integers.

The 2nd term of the sequence is  $-2$   $n=2$

The 4th term of the sequence is  $12$   $n=4$

(a) Find the 6th term of the sequence.

$$\begin{aligned} \textcircled{1} \quad 4a + 2b &= -2 & \times 2 & \quad 8a + 4b = -4 \\ \textcircled{2} \quad 16a + 4b &= 12 & & \quad 16a + 4b = 12 \end{aligned}$$

$$8a = 16$$

$$a = 2$$

into  $\textcircled{1}$

$$8 + 2b = -2$$

$$2b = -10$$

$$b = -5$$

$n$ th term formula  $2n^2 - 5n$

when  $n=6$   $2(6)^2 - 5(6)$

$$\begin{aligned} 2(36) - 30 \\ 72 - 30 &= 42 \end{aligned}$$

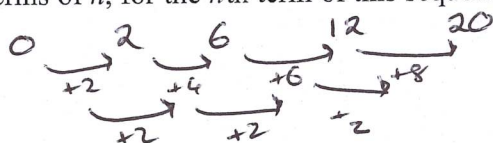
42

(4)

Here are the first five terms of a different quadratic sequence.

0      2      6      12      20

(b) Find an expression, in terms of  $n$ , for the  $n$ th term of this sequence.



$n^2$       1      4      9      16      25

$S$       -1      -2      -3      -4      -5



$$-1n + 0$$

$$n^2 - n$$

$n^2 - n$

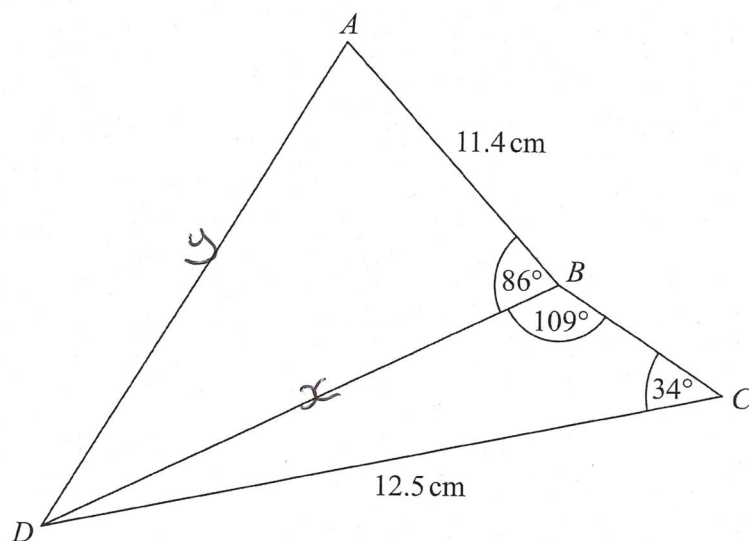
(2)

(Total for Question 16 is 6 marks)





17



Work out the length of  $AD$ .  
Give your answer correct to 3 significant figures.

$$\frac{x}{\sin 34} = \frac{12.5}{\sin 109}$$

$$x = \frac{12.5 \sin 34}{\sin 109}$$

$$x = 7.392674$$

$$y^2 = x^2 + 11.4^2 - 2(x)(11.4)\cos(86)$$

$$y^2 = 172.85$$

$$y = 13.1473$$

$$= 13.1$$

13.1

cm

(Total for Question 17 is 5 marks)



P 4 8 8 6 4 A 0 1 9 2 4

- 18 (a) Show that the equation  $x^3 + x = 7$  has a solution between 1 and 2

$$x^3 + x - 7 = 0$$

$$x=1 \quad 1^3 + 1 - 7 = -5$$

$$x=2 \quad 2^3 + 2 - 7 = 3$$

Sign change so solution between 1 and 2 as required.

(2)

- (b) Show that the equation  $x^3 + x = 7$  can be rearranged to give  $x = \sqrt[3]{7-x}$

$$x^3 = 7 - x$$

$$x = \sqrt[3]{7-x}$$

(1)

- (c) Starting with  $x_0 = 2$ , use the iteration formula  $x_{n+1} = \sqrt[3]{7-x_n}$  three times to find an estimate for a solution of  $x^3 + x = 7$

$$x_0 = 2$$

$$x_1 = \sqrt[3]{7-2} = 1.709975$$

$$x_2 = \sqrt[3]{7-1.70\dots} = 1.7424188$$

$$x_3 = \sqrt[3]{7-1.74\dots} = 1.7388$$

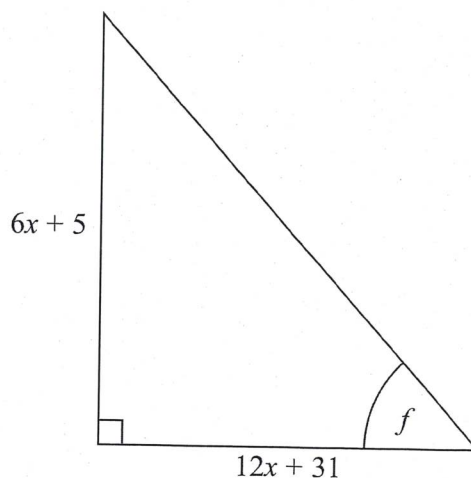
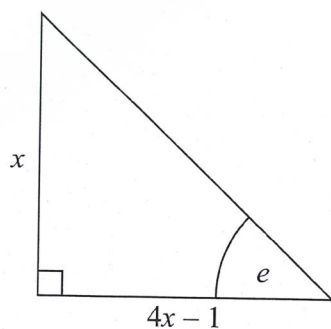
1.74

(3)

(Total for Question 18 is 6 marks)



19 Here are two right-angled triangles.



Given that

$$\tan e = \tan f$$

find the value of  $x$ .

You must show all your working.

$$\tan e = \frac{x}{4x-1}$$

$$\tan f = \frac{6x+5}{12x+31}$$

Since  $\tan e = \tan f$

$$\frac{x}{4x-1} = \frac{6x+5}{12x+31}$$

$$12x^2 + 31x = (6x+5)(4x-1)$$

$$12x^2 + 31x = 24x^2 + 20x + 6x - 5$$

$$0 = 12x^2 - 17x - 5$$

$$\frac{-60}{-20+3}$$

$$= 12x^2 + 3x \mid -20x - 5$$

$$3x(4x+1) \mid -5(4x+1)$$

$$(3x-5) \mid (4x+1)$$

$$x = \frac{5}{3}$$

$$x = \frac{1}{4}$$

$$\frac{5}{3}$$

Since a length  $x = \frac{5}{3}$

(Total for Question 19 is 5 marks)





20 50 people were asked if they speak French or German or Spanish.

Of these people,

31 speak French

2 speak French, German and Spanish

4 speak French and Spanish but not German

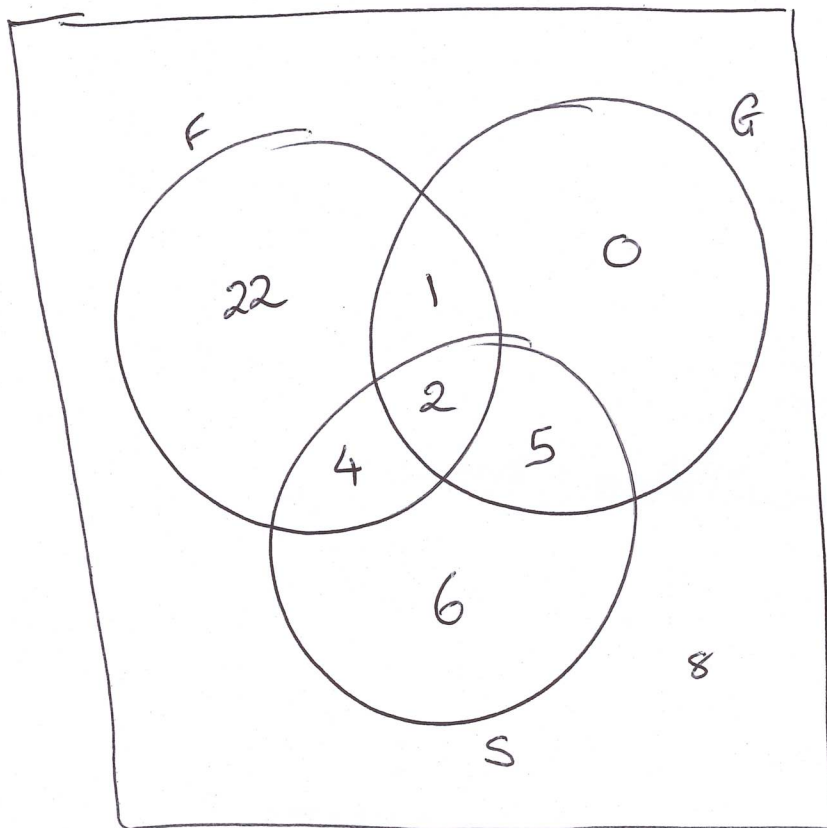
7 speak German and Spanish

8 do not speak any of the languages

all 10 people who speak German speak at least one other language

Two of the 50 people are chosen at random.

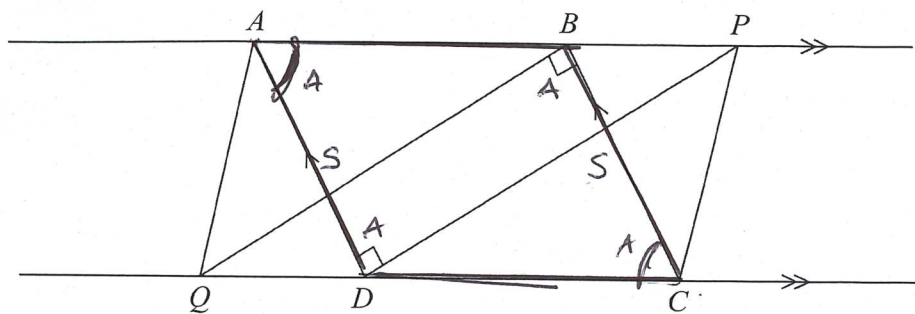
Work out the probability that they both only speak Spanish.



$$\frac{6}{50} \times \frac{5}{49} = \frac{30}{2450}$$
$$= \frac{3}{245}$$

(Total for Question 20 is 5 marks)





$ABCD$  is a parallelogram.  
 $ABP$  and  $QDC$  are straight lines.  
 Angle  $ADP = \text{angle } CBQ = 90^\circ$

(a) Prove that triangle  $ADP$  is congruent to triangle  $CBQ$ .

$\angle ADP = \angle CBQ$  as given  
 $AD = BC$  as opposite sides of a parallelogram  
 $\angle DAP = \angle BCQ$  as opposite angles of a parallelogram  
 $\therefore \triangle ADP \cong \triangle CBQ$  ASA so congruent

(3)

(b) Explain why  $AQ$  is parallel to  $PC$ .

$AP = QC$  as  $\triangle ADP \cong \triangle CBQ$  (above)  
 $AQ$  and  $PC$  are parallel as on straight line with  $AB$  and  $DC$

(2)

(Total for Question 21 is 5 marks)

TOTAL FOR PAPER IS 80 MARKS

